

The Data-as-a-Service Framework for Cyber-Physical-Social Big Data

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1. Hyper (Cyber-Physical-Social) World

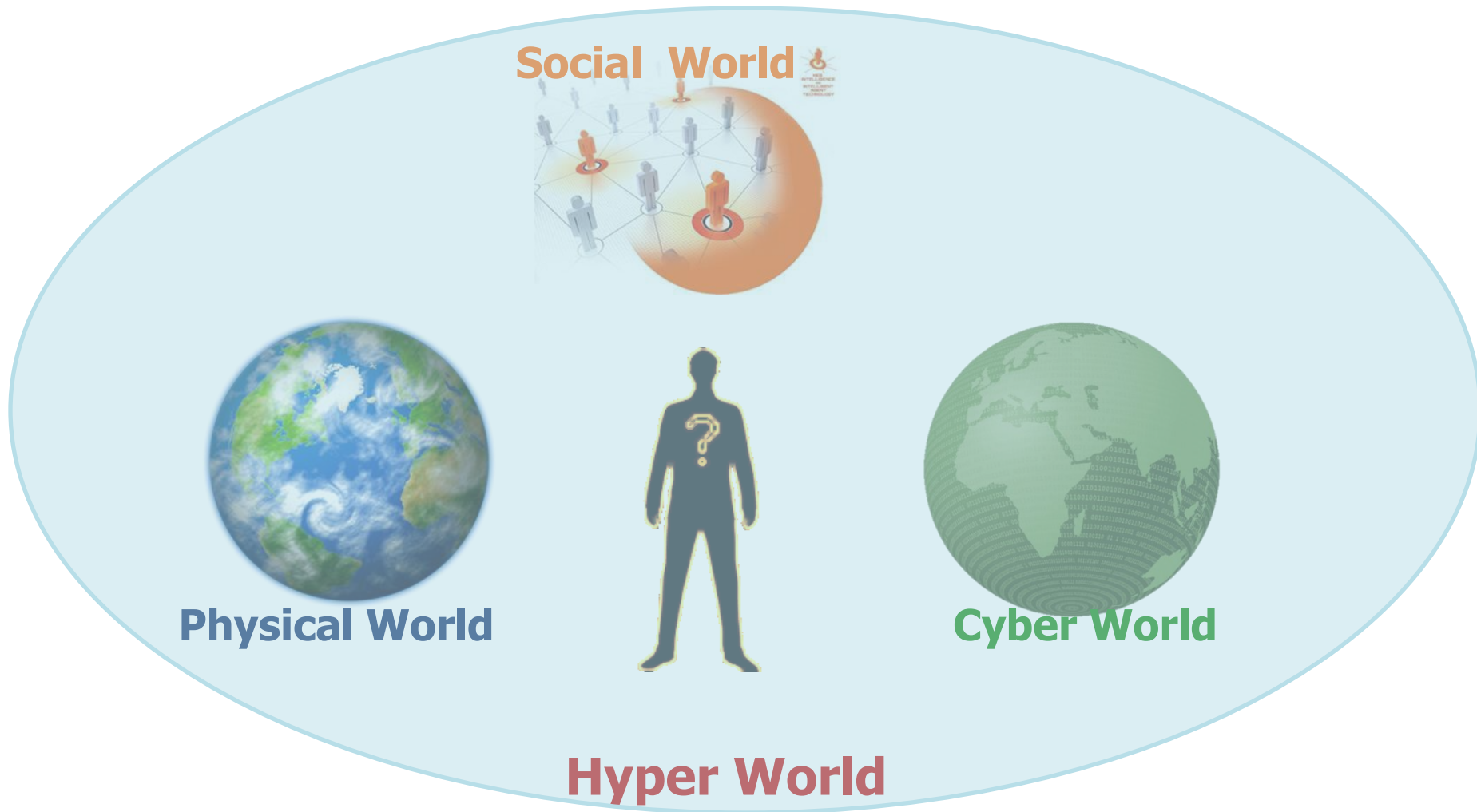
2. Big Data and Challenges

3. A Tensor-Based Approach

4. Illustrations and Examples

5. Conclusion

Hyper (Cyber-Physical-Social) World



What we are and what we can do in the Hyper World?

Hyperspace

- Cyber – computation, communication, and control that are discrete, logical, and switched
- Physical – natural and human-made systems governed by the laws of physics and operating in continuous time
- Social – socially produced space, serves as a tool of thoughts, action, mind, sense, interaction, communications, etc.

Hyperspace = Cyber Space + Physical Space + Social Space

Hyber WORLD

Social Space



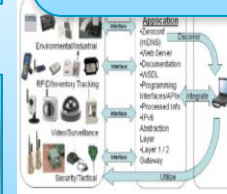
Social Comuting
(Internet of People)
u-Human-Computer
Interface (BCI)



Pervasive/Ubiquitous Intelligence
(hybrid world)



u-things
(Internet of Things)
u-systems/services







Physical Space



Characteristics of Hyperworld

“Its basic characteristic is direct mapping between virtual and real worlds via active devices including sensors, actuators, micro-machines, robots, etc.”

-- Kunii, Ma & Huang, Keynote “Hyperworld Modeling” in VIS’96

-  Data/Info Explosion! Last 5 years’ web data > 5,000 years’ whole data
-  Connection Explosion! C2C → D2D → H2H → M2M → CPS → T2T (IoT)
-  Service/App Explosion! WbS → SaaS → PaaS → IaaS → EaaS → Cloud
-  Intelligence Explosion! Ubi-Sensing → CA → TTT → AmI → Smart W/P

Intelligent Computing Waves

➤ 1st: AI (Logic/KL-based, cyber-based)

- *Machine learning*
- *NLP & Comp-Vision*
- *Robot & game theory*
- *Expert system*
- *Knowledge/Reasoning*
- *DAI (Distributed AI)*

➤ 2nd: Physical-based

- *Probabilistic computing*
- *Fuzzy logic*
- *Neural network*
- *GA/Evolutionary computing*
- *Chaotic/Swarm computing*
- *Biologic computing*

➤ 3rd: Social-based

- *Autonomous software*
- *Multi/Massive agents*
- *Agent language*
- *Agent negotiation & cooperation*
- *Personal/social behavior*
- *Web intelligence/semantics*

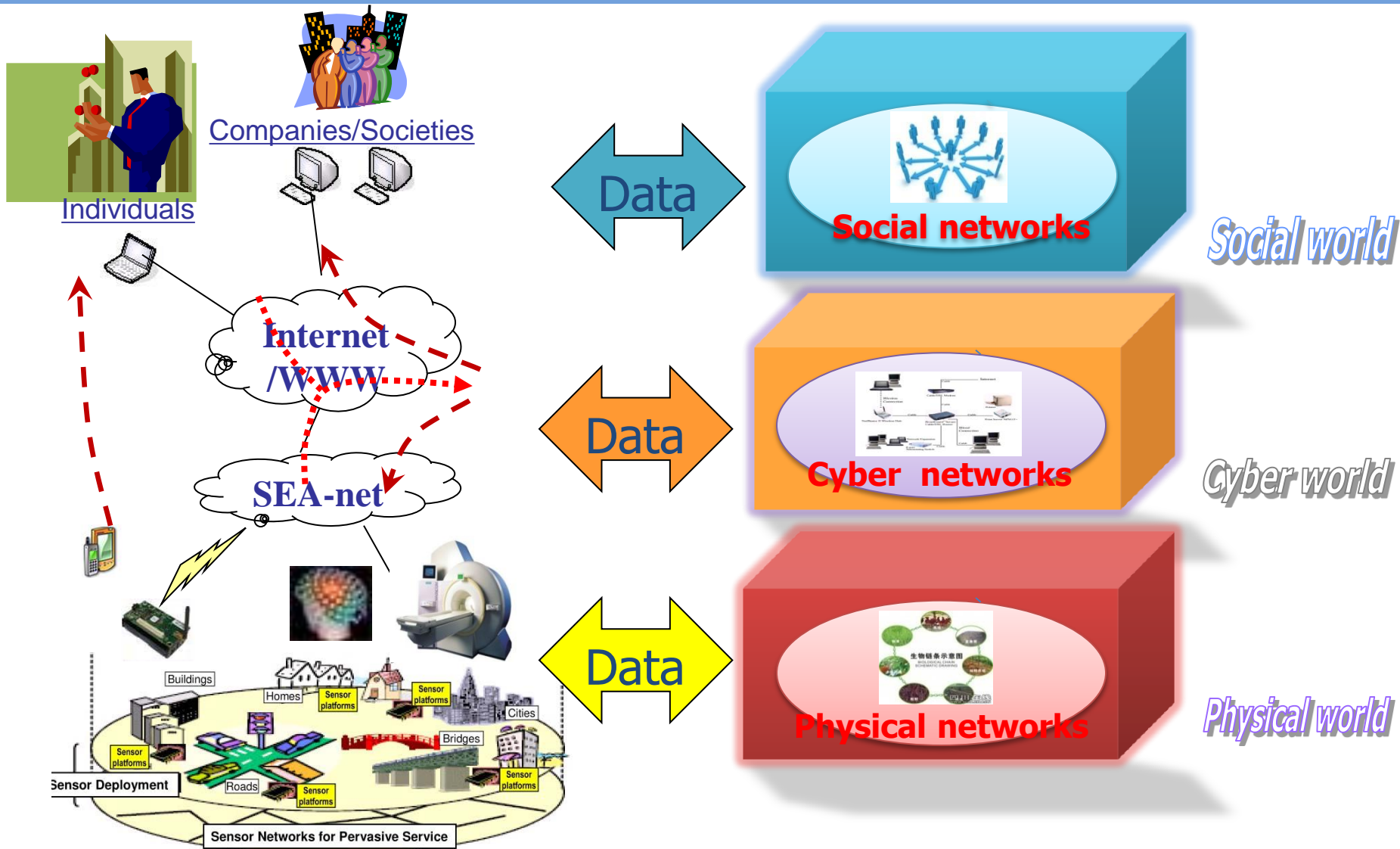
➤ 4th: Cyber-Physical-Social

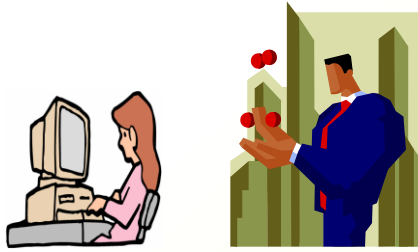
- *Physical/everyday things' intelligence*
- *Atop of the above 3 intelligent comp*
- *Scale, dynamic, heterogeneous, spontaneous*
- *Predictable, controllable, adaptable, manageable, ethic, ...*
- *Others-aware & self-aware → mind/spirit?*

Four Fundamental Issues of HyperWorld

- How to realize the **harmonious symbiosis** of humans, information and things in the hyper world?
- How to implement the **data-cycle** system as a practical way to realize the harmonious symbiosis of humans, information and things in the hyper world?
- How to investigate **intelligence** from a **holistic way** in the hyper world?
- How to do unifying studies of **humans, networks** and information **granularity** in the hyper world?

HyperWorld





Individuals

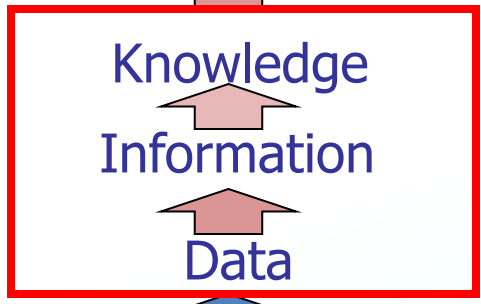
Agents



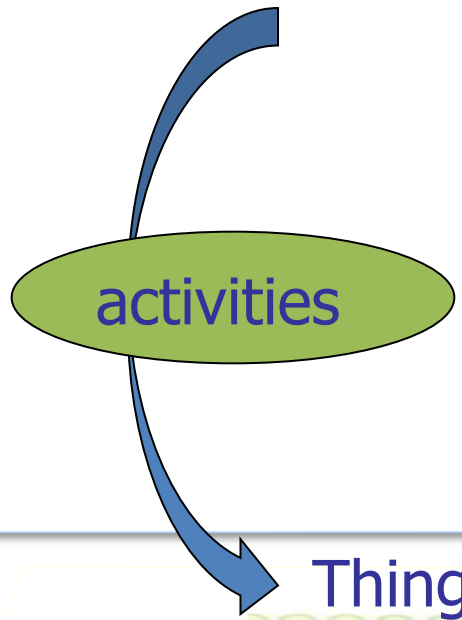
Human



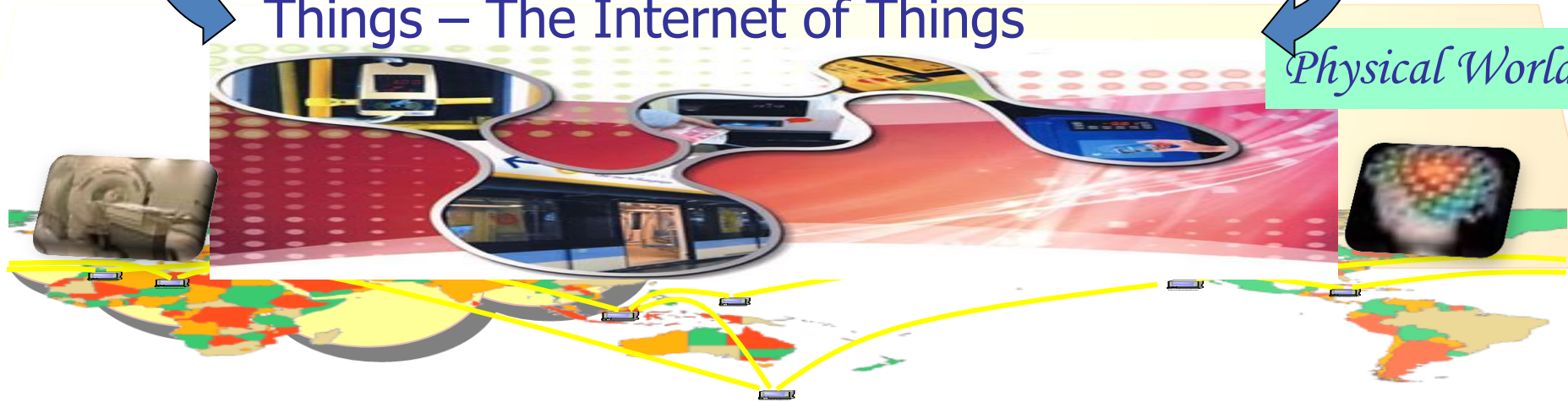
Companies/Societies
Socio-culture & organizational components

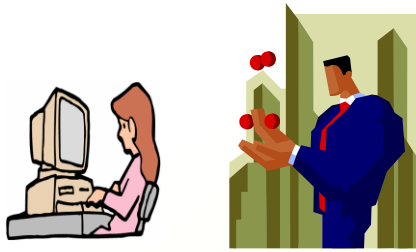


Data Cycle



Things – The Internet of Things





Individuals

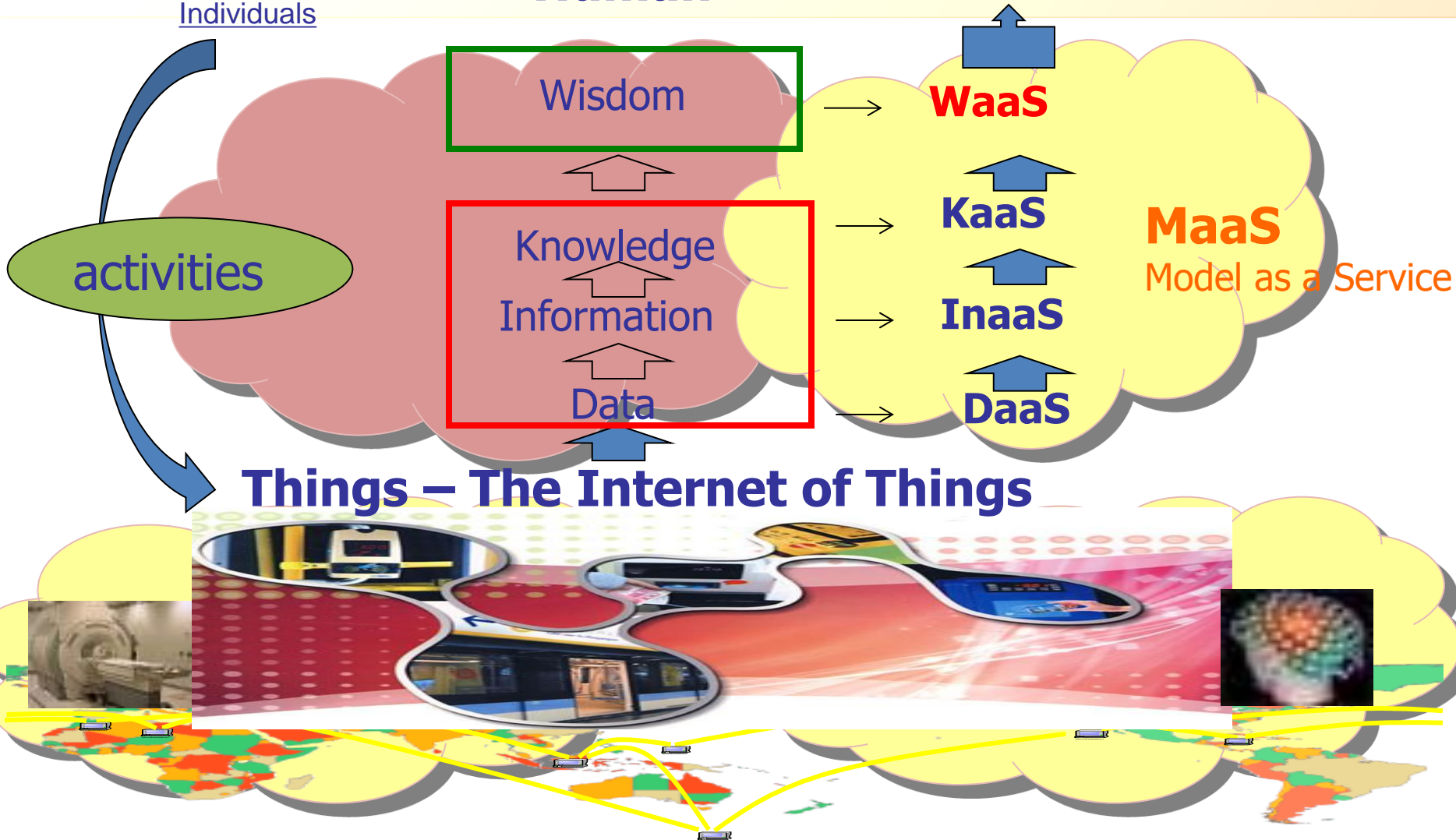
Agents



Human



Companies/Societies
Socio-culture &
organizational components





1. Smart Word and Hyper World



2. Big Data and Challenges



3. A Tensor-Based Approach



4. Illustrations and Examples



5. Conclusion

What's the difference between large data and big data?



Just Size?

Features of Big Data

4Vs Features

■ Volume

Terabytes, Petabytes,...

■ Variety

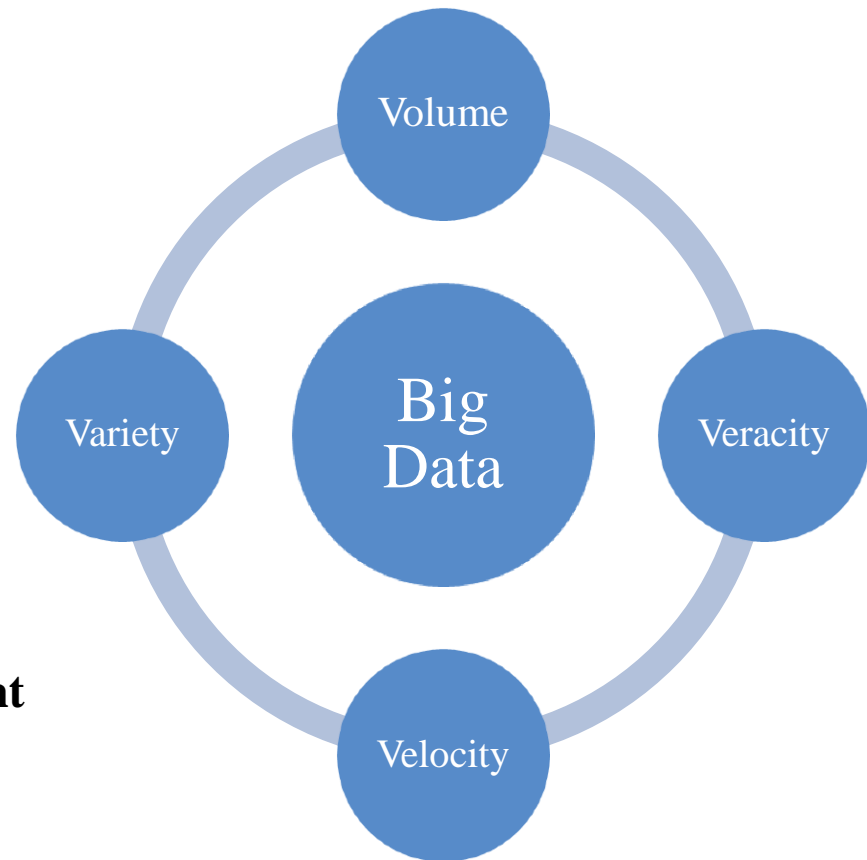
Structured
Semi-Structured
Un-Structured

■ Velocity

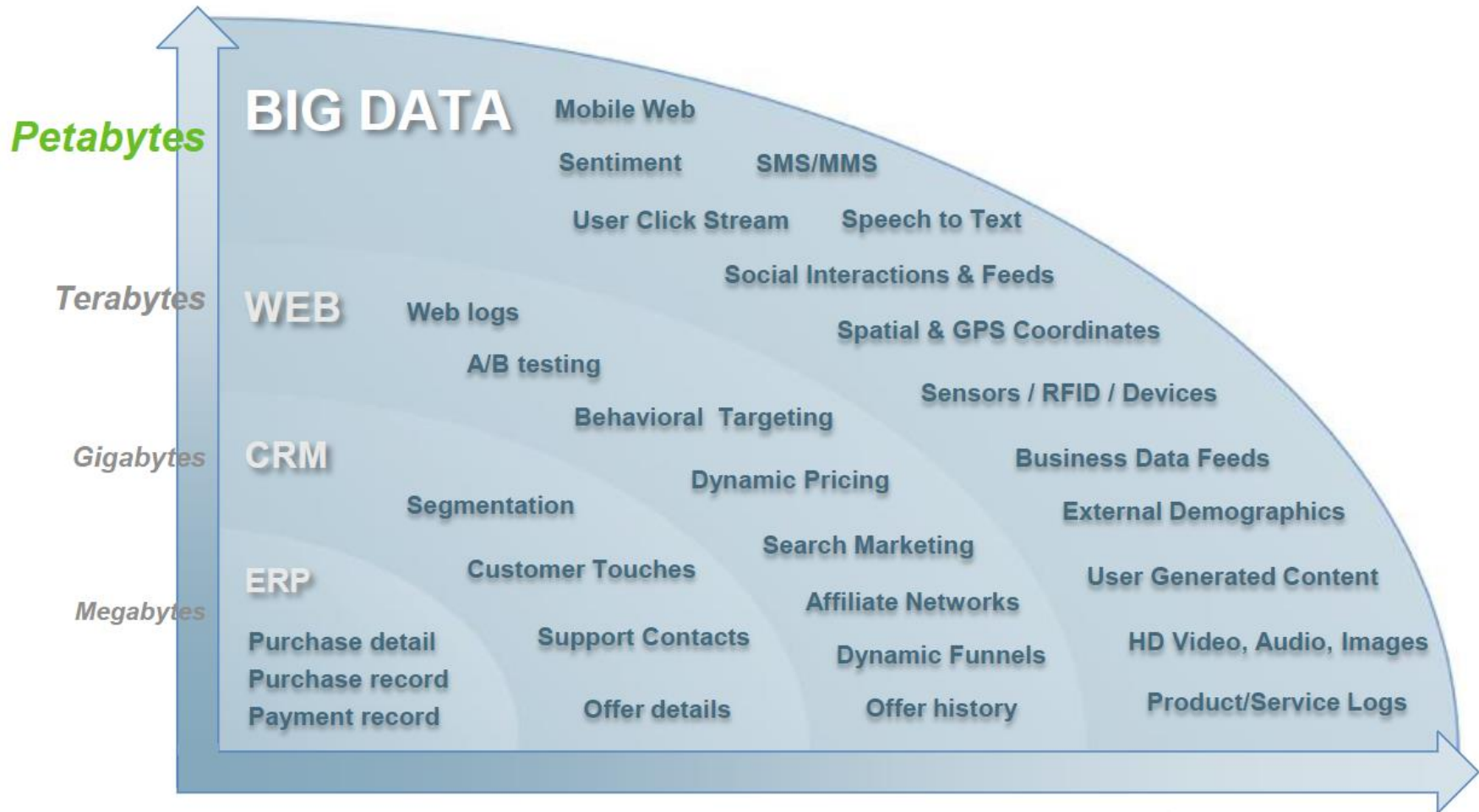
Streaming Data
Processing time requirement

■ Veracity

Quality of Data



Cyber-Physical-Social Data



Challenges Caused by Big Data

Volume

- Large Scale Data , Limited Compute Resources

Variety

- Diversified Format, Unified Representation

Velocity

- Requirement for quick processing

Veracity

- Inconsistent, Incomplete, Redundant Data



How to tackle the problems caused by the 4Vs of Big Data?

1. Smart Word and Hyper World

2. Big Data and Challenges

3. A Tensor-Based Framework

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5. Conclusion

A Tensor-Based Approach

3.1

- Tensor and Tensor Decomposition

3.2

- ‘4Vs Problem’ with Tensor

3.3

- A Framework for Big Data Analysis and Mining

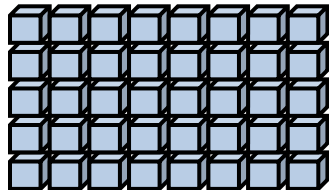
Tensor Definition

Mathematics: Tensor

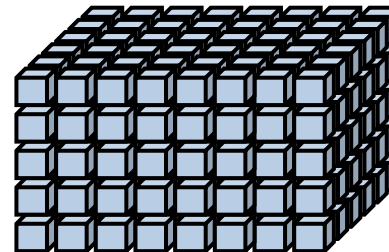
Computer Science: Multiple Dimensional Arrays



One Order Tensor:
Vector



Two Order Tensor:
Matrix



Three Order **Tensor**

Tensor Computations and Algebra

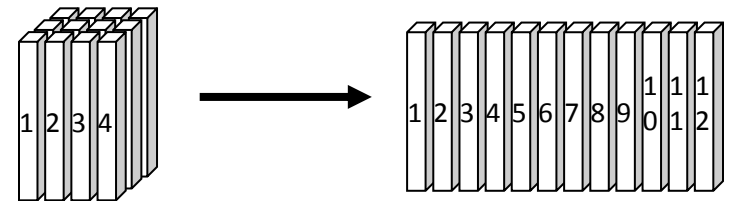
$$\begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} \otimes \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} = \begin{array}{|c|c|c|} \hline 1 & 2 & 3 \\ \hline 3 & 6 & 9 \\ \hline 4 & 8 & 12 \\ \hline \end{array}$$

$(\mathcal{A} \otimes \mathcal{B})_{i_1, i_2, \dots, i_m, j_1, j_2, \dots, j_n} = \mathcal{A}_{i_1, i_2, \dots, i_m} * \mathcal{B}_{j_1, j_2, \dots, j_n}$

- Kronecker product.
- Tensor-tensor product
- Inverse
- Identity tensor
- Transpose
- Tensor-matrix mode product
- Stefan Ragnarsson, Ph.D thesis, 2012, Cornell

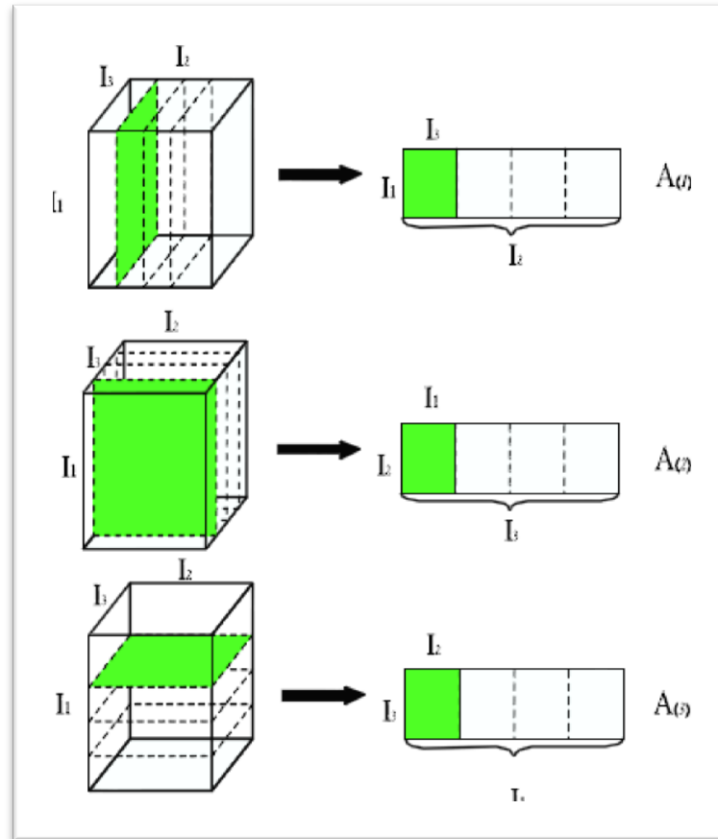
$$\mathcal{A} \times_i \mathcal{B} = \text{fold}_i(\mathcal{B} * \text{unfold}_i(\mathcal{A}))$$

Equivalently: $(\mathcal{A} \times_i \mathcal{B})_{j_{1:i-1}, k, j_{i+1:r}} = \sum_{\ell=1}^{d_i} \mathcal{A}_{j_{1:i-1}, \ell, j_{i+1:r}} \mathcal{B}_{k, \ell}$



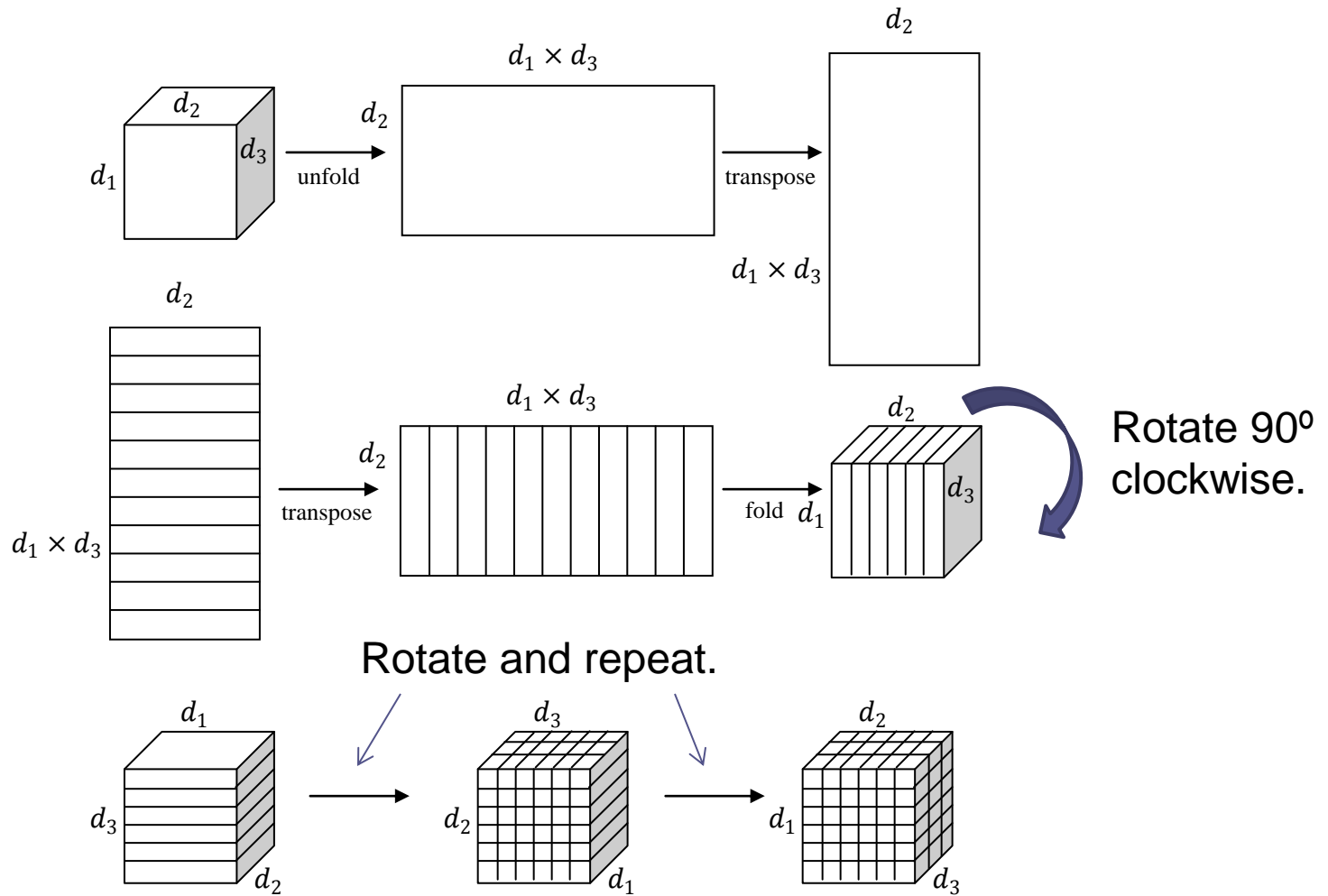
Unfolding on mode 1 (take mode 1 fibers and linearize).

Illustration



Model-N Unfolding

Illustration

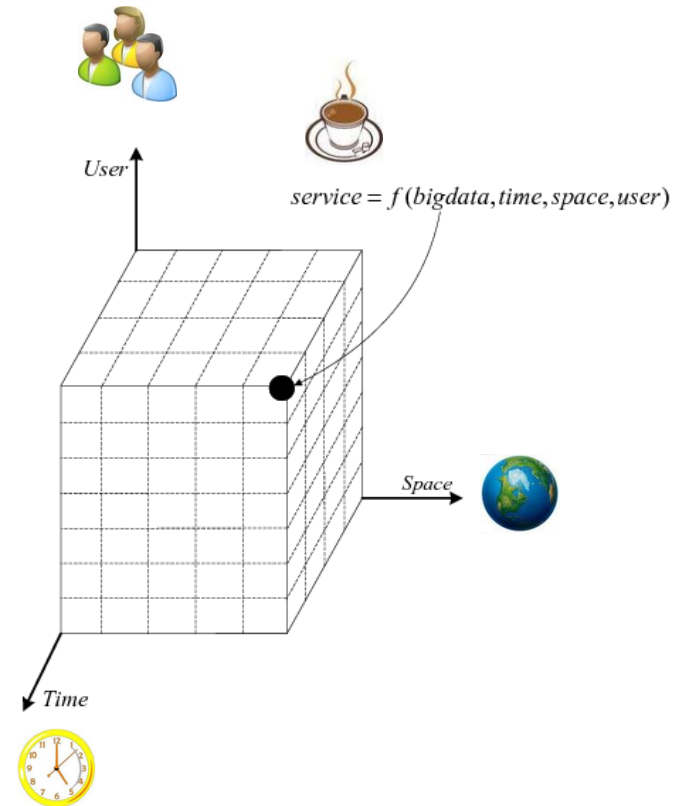


Formal Description

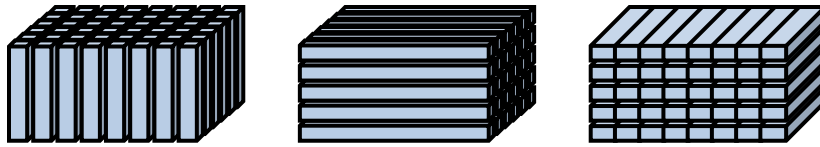
$$A \in \mathcal{R}^{I_t \times I_x \times I_y \times I_z \times I_c \times I_u}$$

$$a_{ijklmn}, i \in I_t, j \in I_x, k \in I_y, l \in I_z, m \in I_c, n \in I_u$$

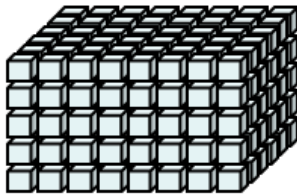
where \mathcal{R} is defined on the real number domain; $I_t, I_x, I_y, I_z, I_c, I_u$ refer to the dimensions on time, space coordinates (I_x, I_y, I_z) and cyber resources. $I_t \times I_x \times I_y \times I_z \times I_c \times I_u$ denotes the Cartesian product operation of $I_t, I_x, I_y, I_z, I_c, I_u$. The value of each



Tensor Decomposition



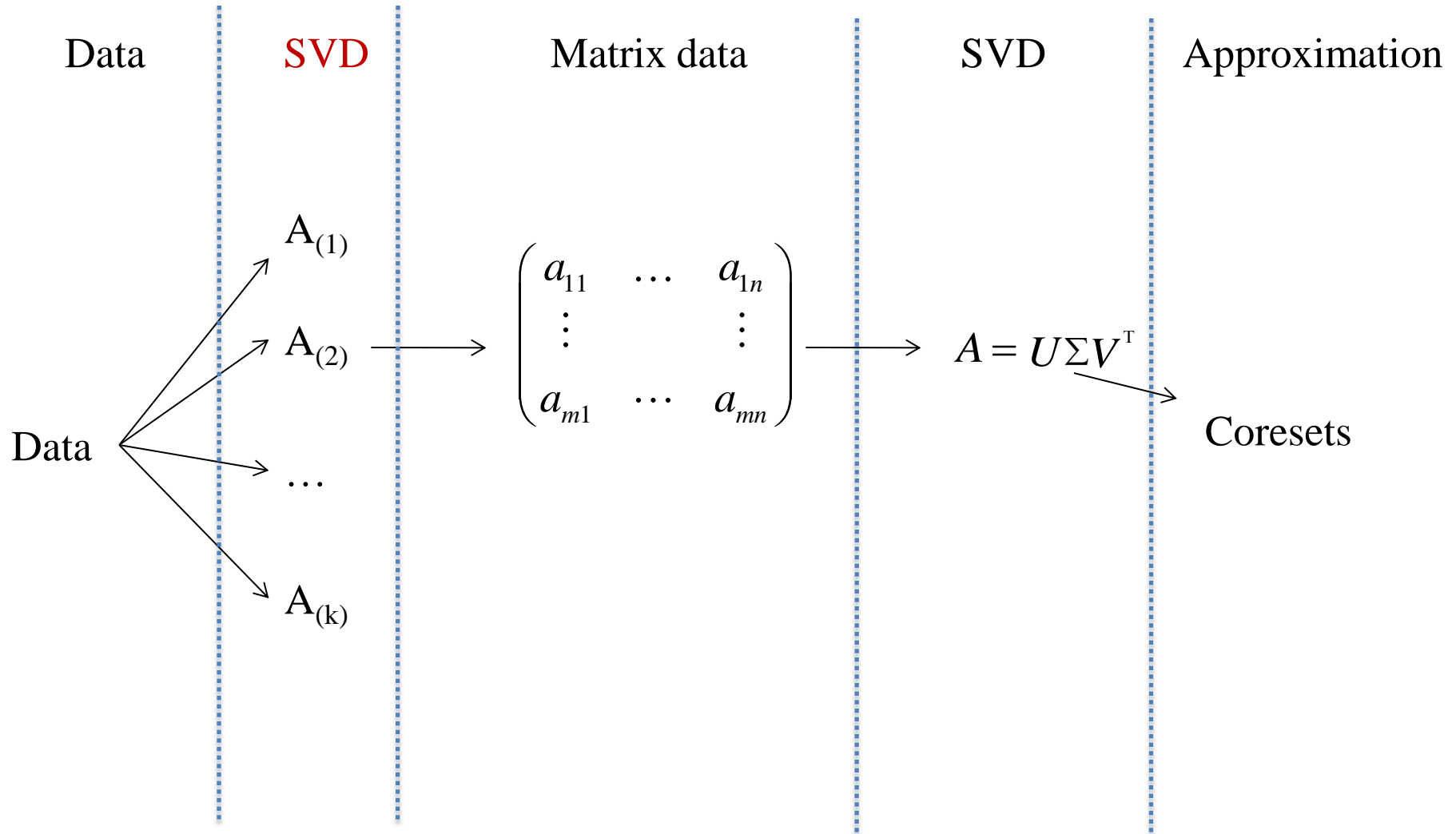
Tensor decomposition is an important data processing tool.



Big data are modeled as tensors



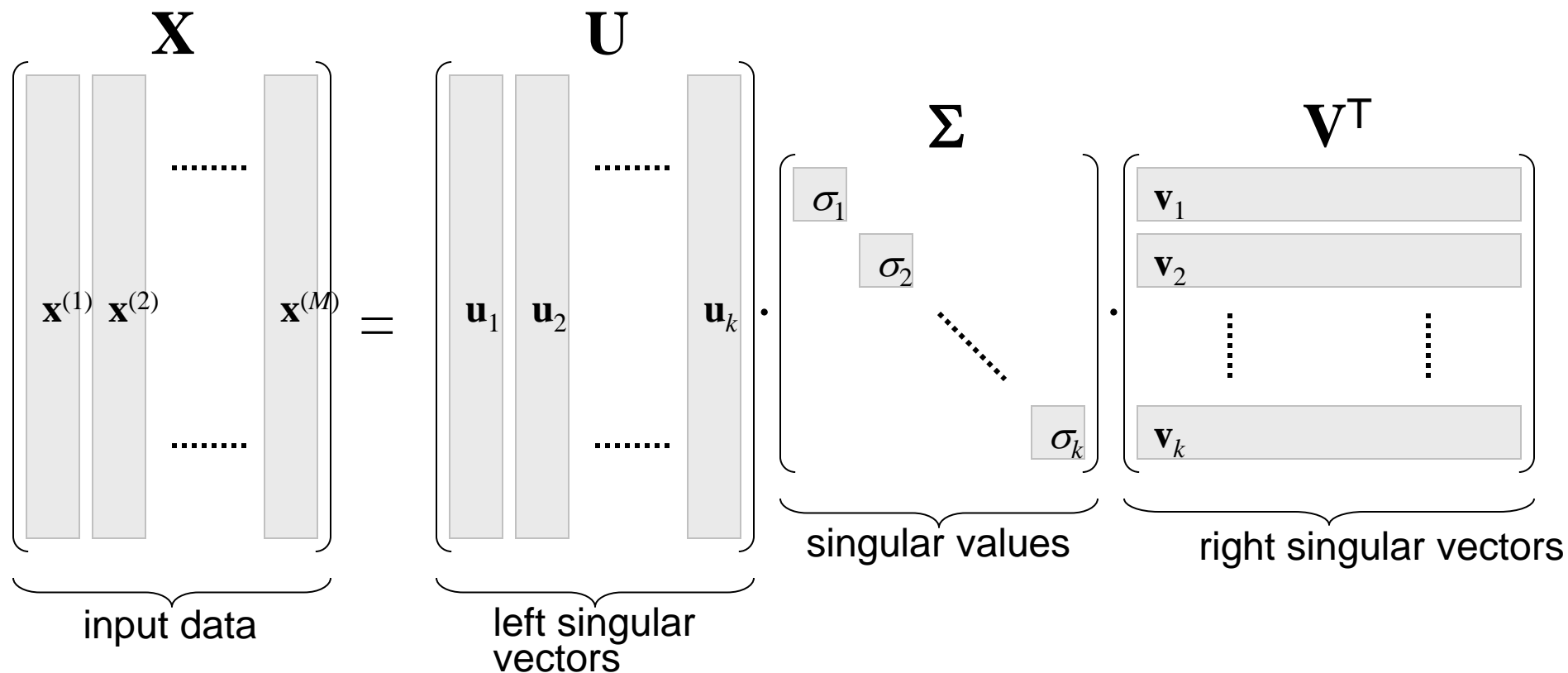
Decomposition Process





Singular Value Decomposition (SVD)

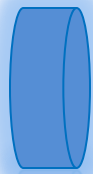
$$\mathbf{X} = \mathbf{U}\mathbf{\Sigma}\mathbf{V}^T$$



Incremental SVD

Update the singular vectors and singular values by using the incremental decomposition results of matrix A_1

$$A_0 = U \Sigma V^T$$



Incremental Matrix

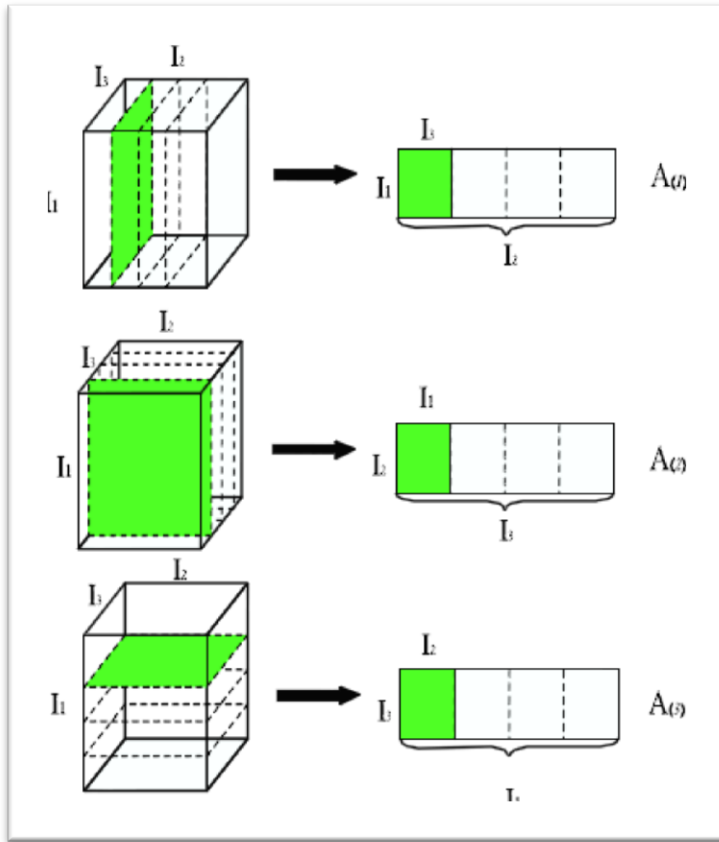
$$\begin{bmatrix} A_0 & A_1 \end{bmatrix} = \underbrace{\begin{bmatrix} U & J \end{bmatrix}}_{\text{Updated U}} U' \underbrace{\Sigma'}_{\text{Updated } \Sigma} \underbrace{V'^T \begin{pmatrix} V & 0 \\ 0 & I \end{pmatrix}^T}_{\text{Updated V}}$$

Updated U

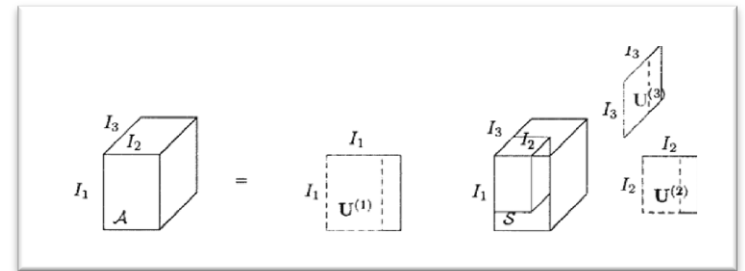
Updated V

Updated Σ

HO-SVD Tensor Decomposition



Model-N Unfolding



Approximation Assemble

Approximate Tensor Calculation

Matrix Unfolding

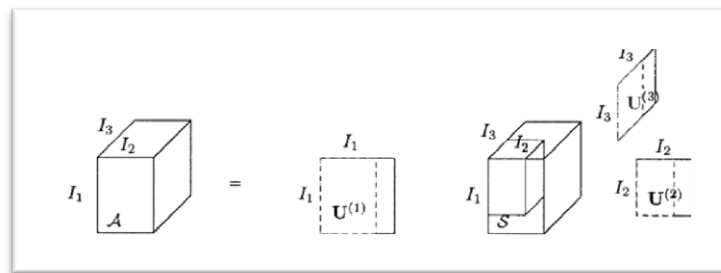
$$A_1 \in R^{I_1 \times I_2 I_3}$$

$$A_2 \in R^{I_2 \times I_1 I_3}$$

$$A_3 \in R^{I_1 I_2 \times I_3}$$

SVD for Every Unfolding Matrix

$$A_i = U_i \Sigma V_i^T$$



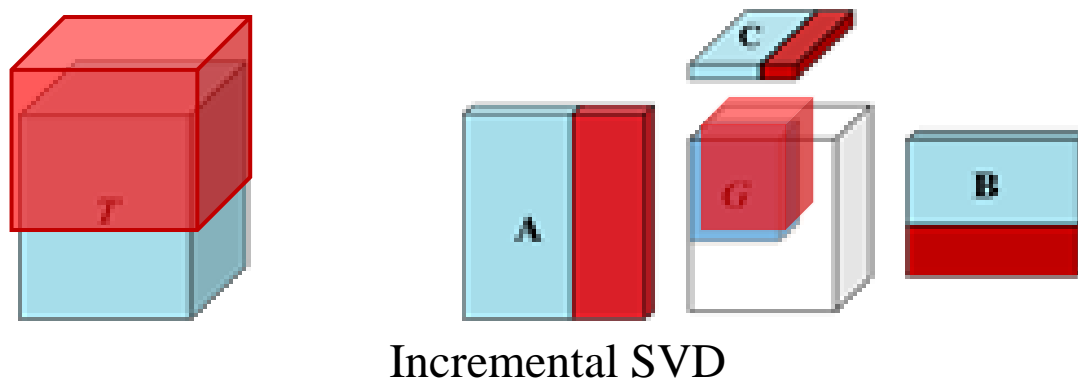
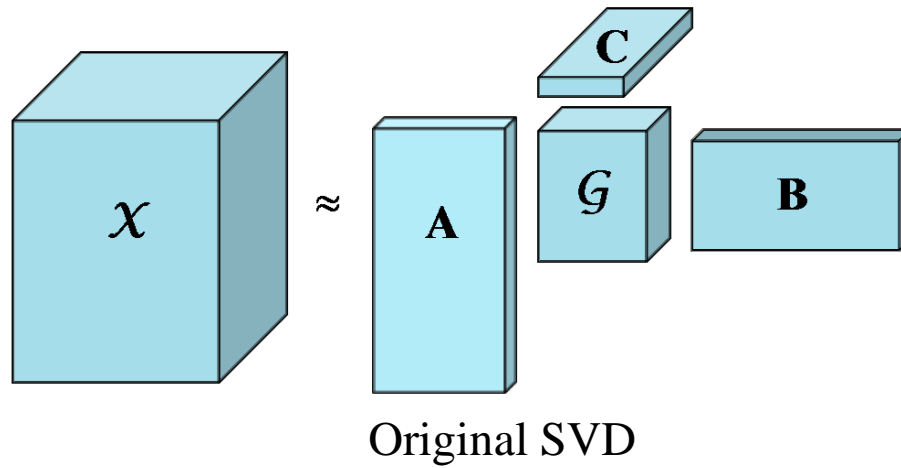
Approximate Tensor

$$\tilde{A} = S \times_1 U_{c_1}^{(t)} \times_2 U_{c_2}^{(x)} \times_3 U_{c_3}^{(y)} \times_4 U_{c_4}^{(z)} \times_5 U_{c_5}^{(c)} \times_6 U_{c_6}^{(u)}$$

Core Tensor

$$S = A \times_1 (U_{c_1}^{(t)})^T \times_2 (U_{c_2}^{(x)})^T \times_3 (U_{c_3}^{(y)})^T \times_4 (U_{c_4}^{(z)})^T \times_5 (U_{c_5}^{(c)})^T \times_6 (U_{c_6}^{(u)})^T$$

Incremental HOSVD



A Tensor-Based Approach

3.1

- Tensor and Tensor Decomposition

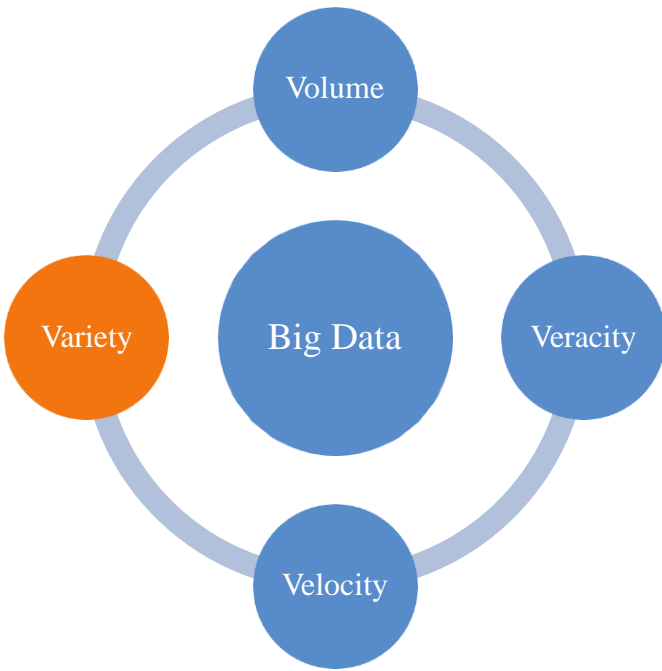
3.2

- ‘4Vs Problem’ with Tensor

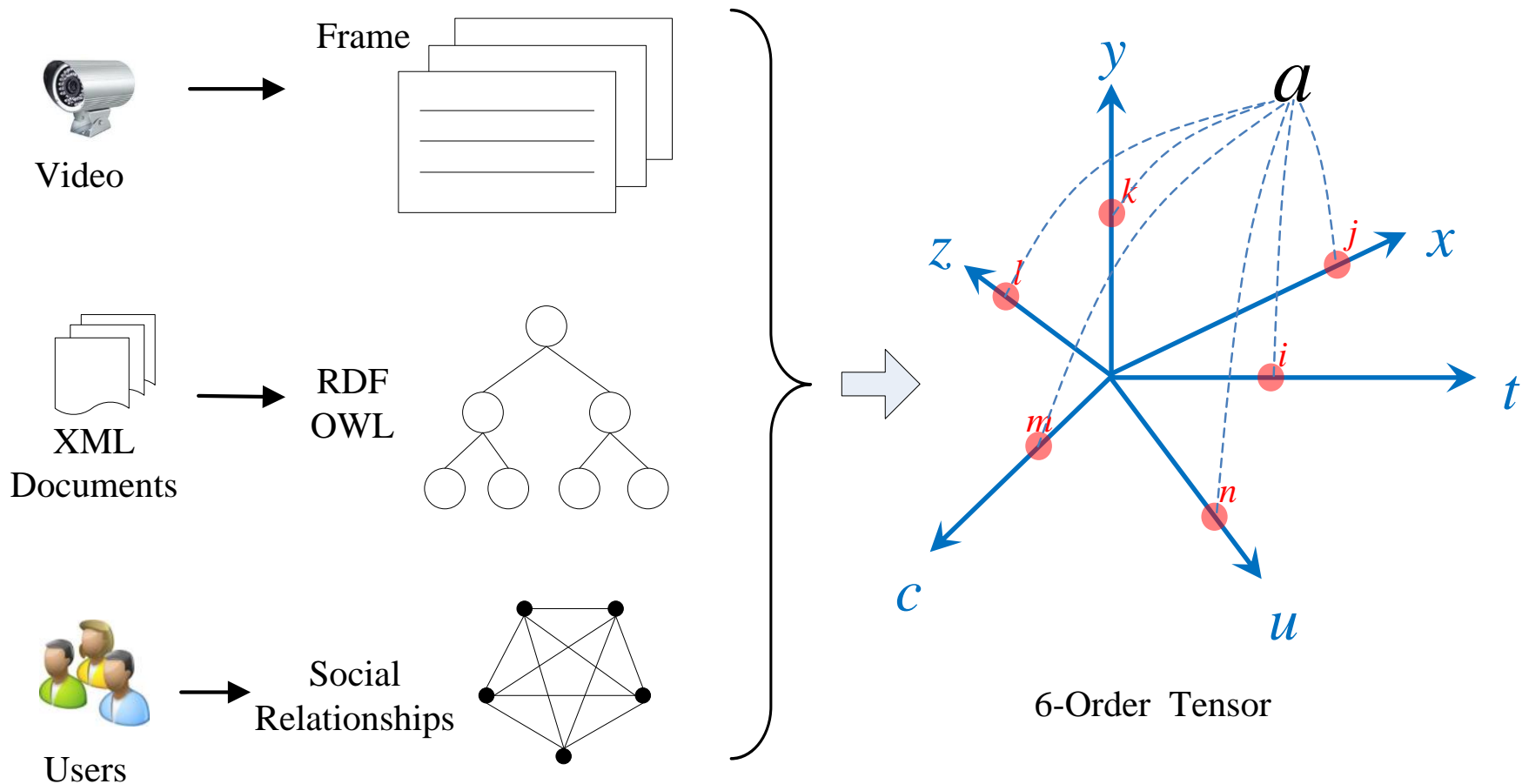
3.3

- A Framework for Big Data Analysis and Mining

Variety

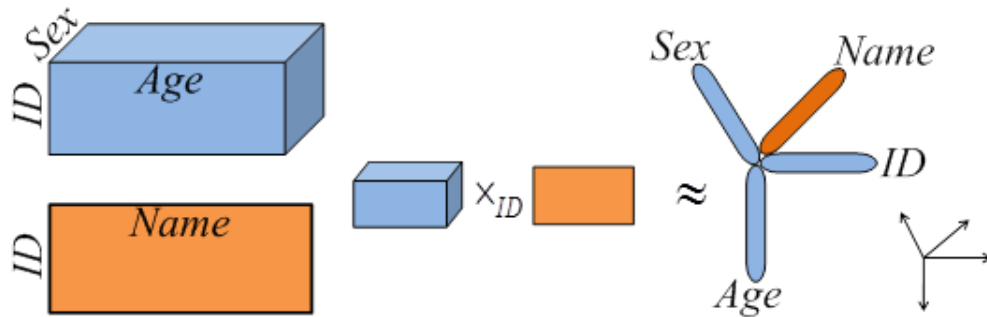


$$f : (d_u \cup d_{semi} \cup d_s) \rightarrow \underbrace{T_u \cup T_{semi} \cup T_s}_T$$

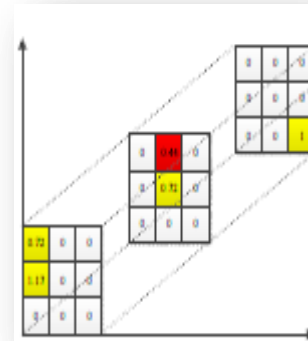
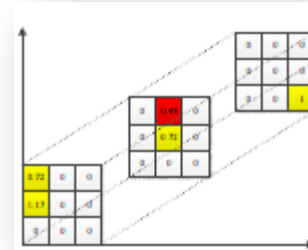
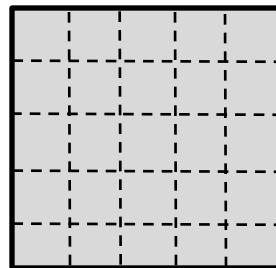
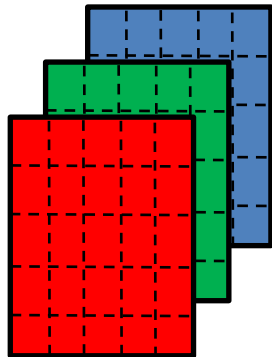
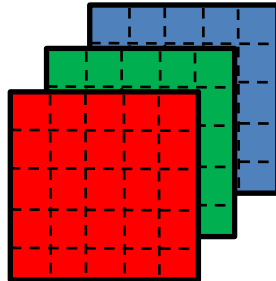
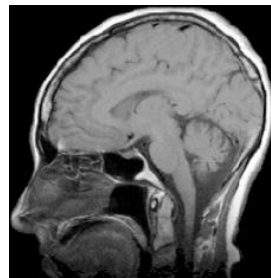
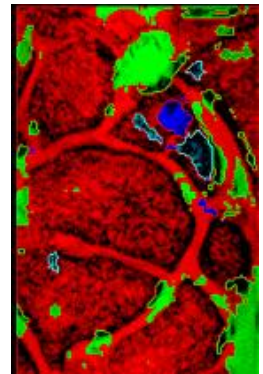
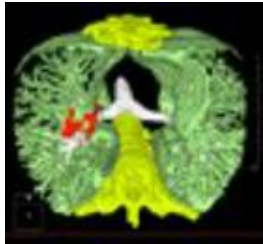


ID	Age	Sex
1	31	M
2	29	F
3	6	M

ID	Name
1	Charles
2	Alice
3	Bob



Variety



$$\begin{pmatrix} 201 & 76 & 44 \\ 234 & 123 & 67 \\ 9 & 134 & 84 \end{pmatrix}$$

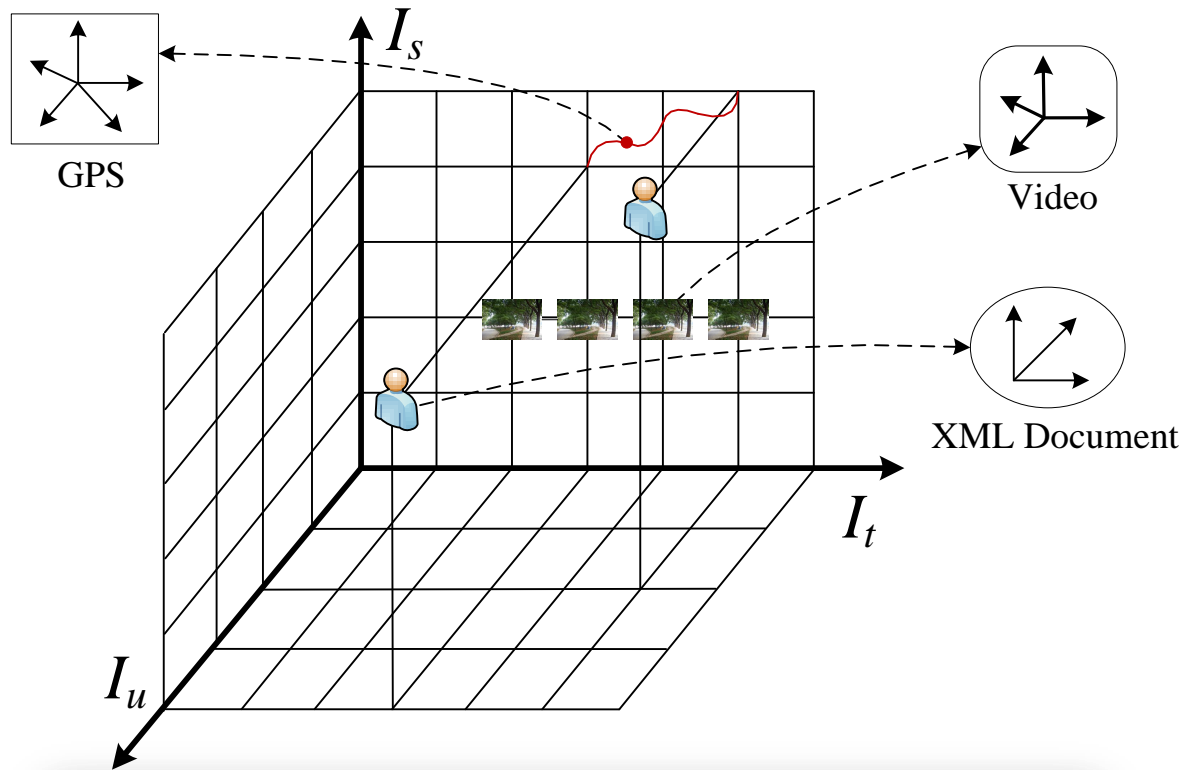
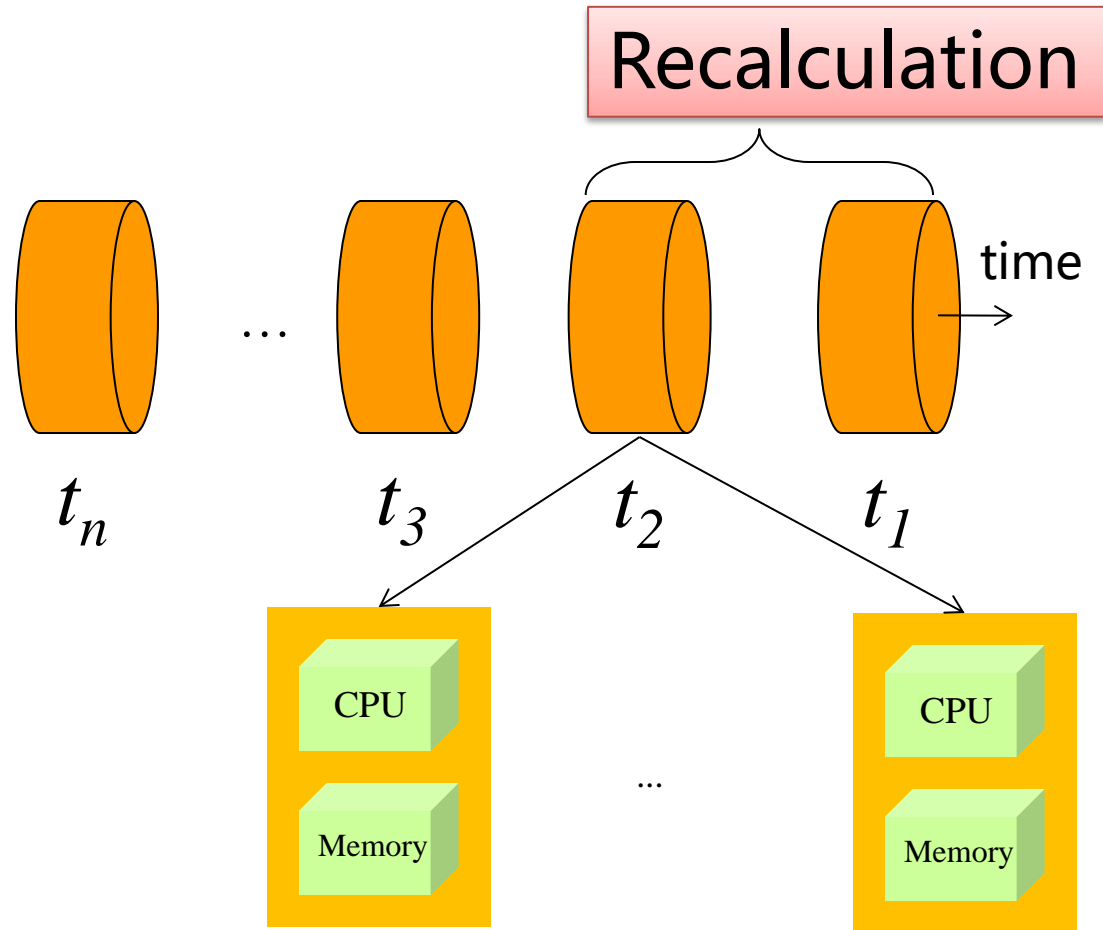
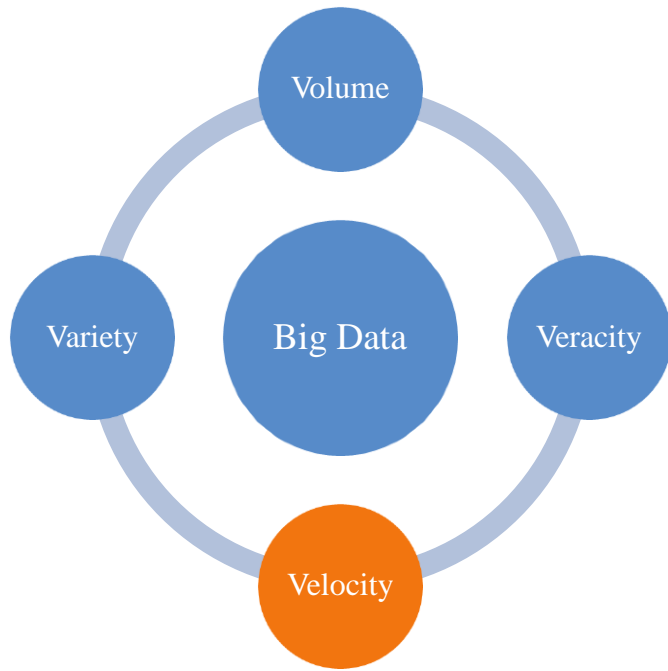
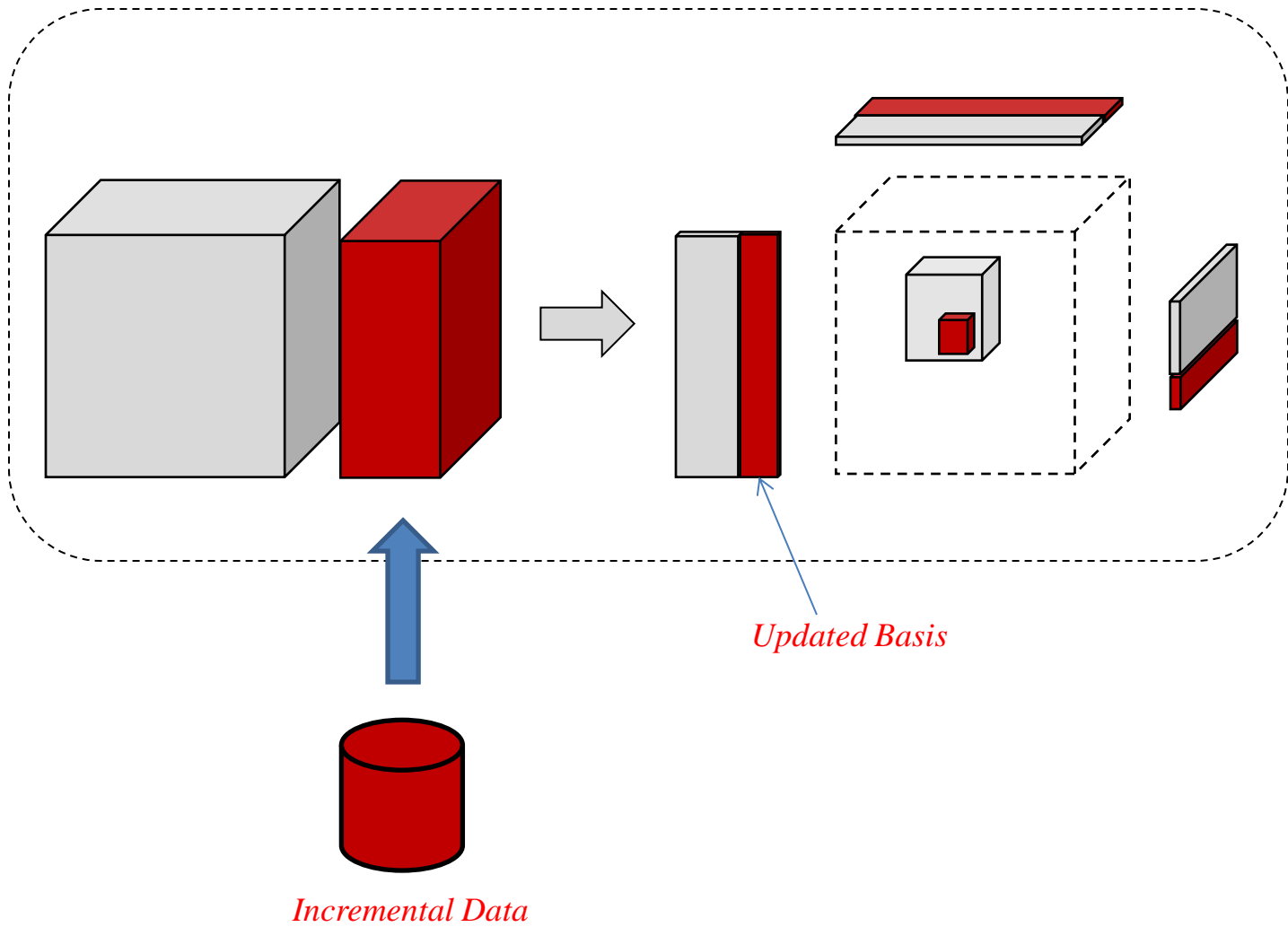


Fig. 8. Using the tensor extension operator, the sub-tensors are integrated together to a higher unified tensor.

Unified Representation for Big Data

Velocity





Incremental HO-SVD

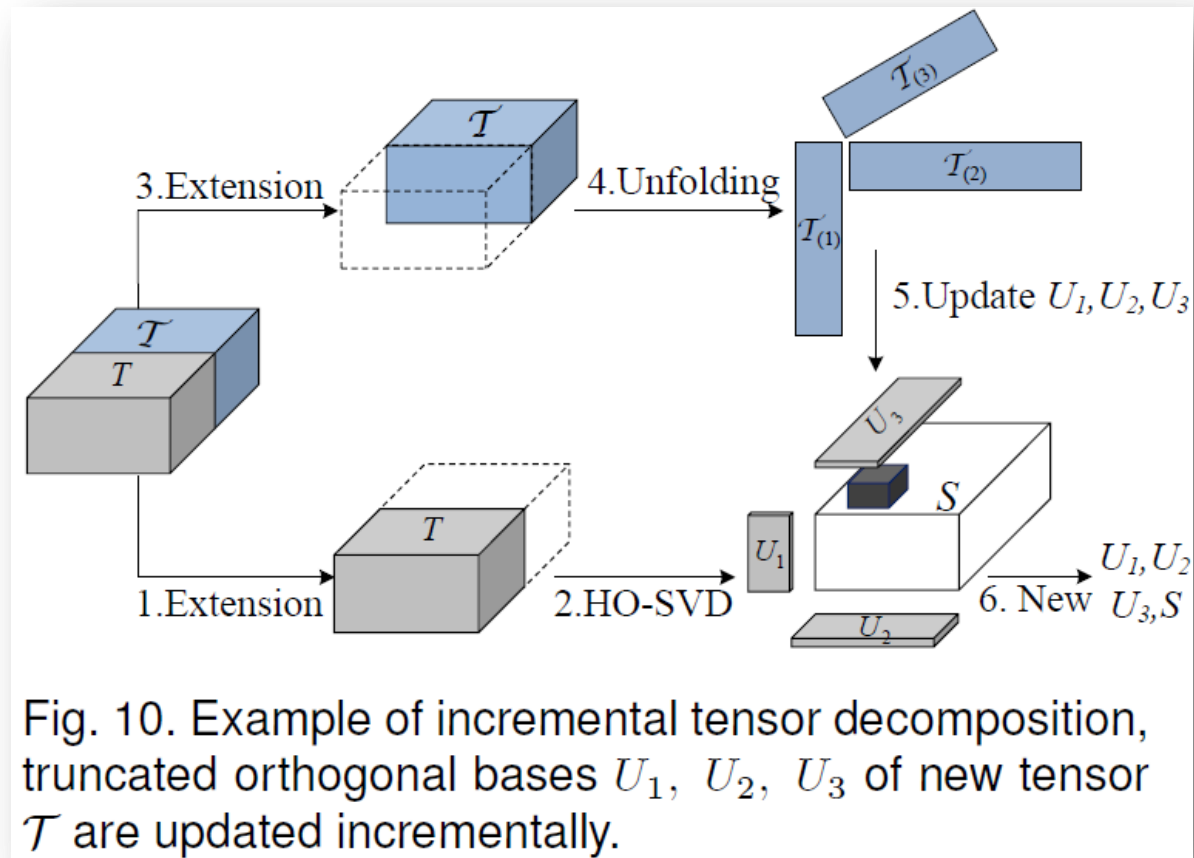
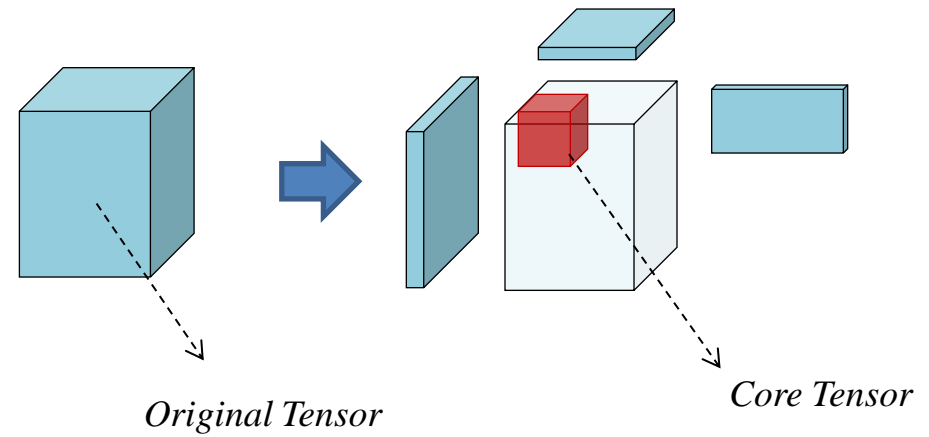
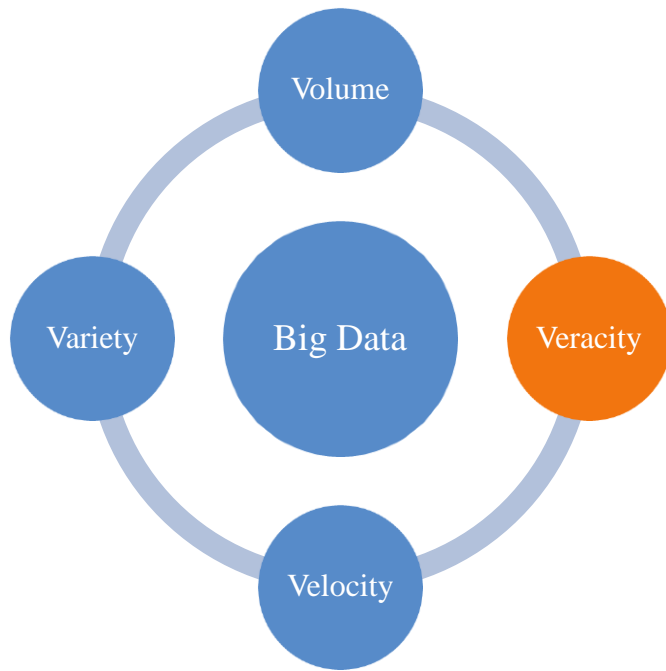


Fig. 10. Example of incremental tensor decomposition, truncated orthogonal bases U_1 , U_2 , U_3 of new tensor T are updated incrementally.

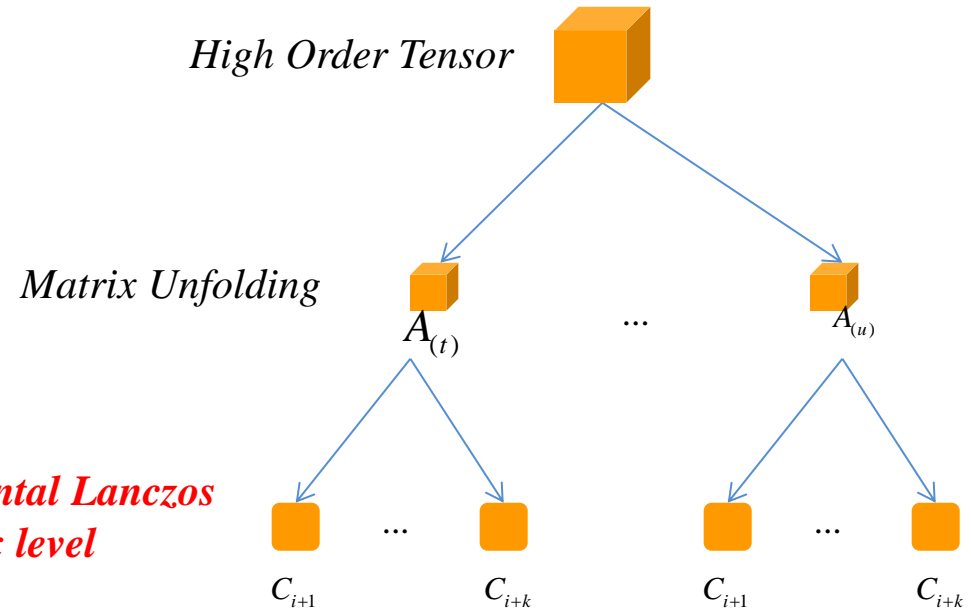
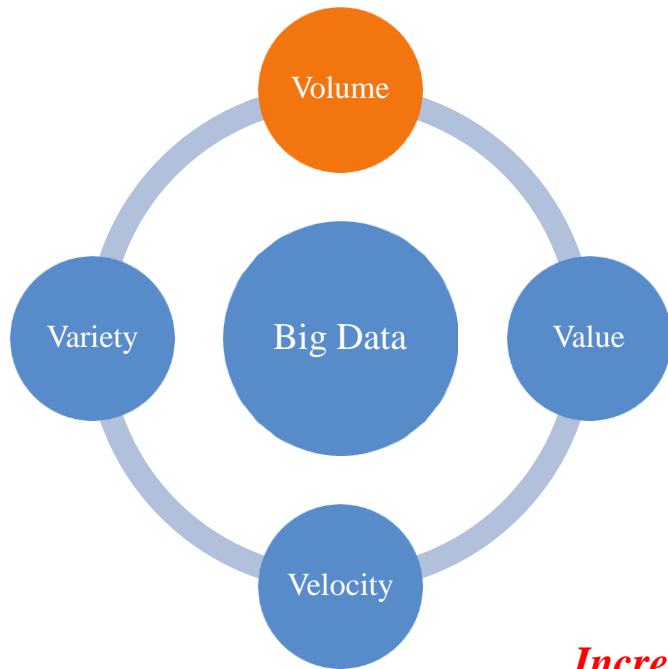


Extract High Quality Core Tensor from PB(TB) Level Medial Tensor

Error Constraints

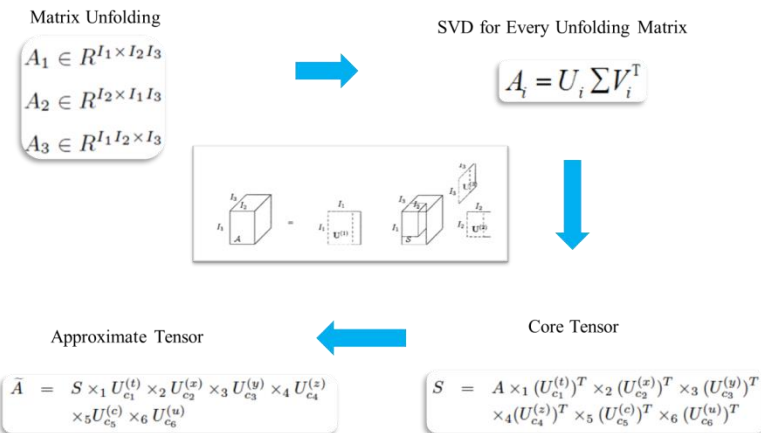
$$\min_{\chi \in \lambda(A)} |\theta_i - \chi| \leq |\beta_k| \cdot |s_{ki}|, i = 1 : k \quad \|T\|_F = \left(\sum_{ijklmn} a_{ijklmn}^2 \right)^{\frac{1}{2}}$$

$$\max_{U_i} \|T \times_t U_t^T \times_x U_x^T \times_y U_y^T \times_z U_z^T \times_r U_r^T \times_u U_u^T\|_F^2$$



**Incremental Lanczos
at matrix level**

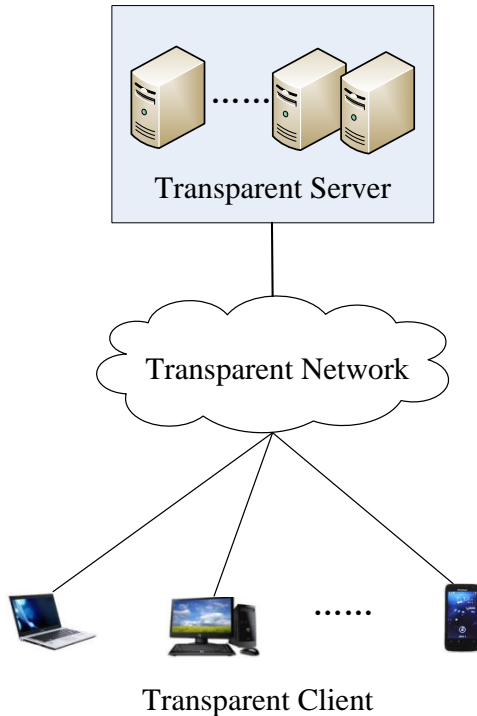
Two layers incremental SVD parallel
strategies on servers



Transparent Computing vs. Cloud Computing

Computation in sever:

- Synthetic SVD Results
- Compute Core Tensor

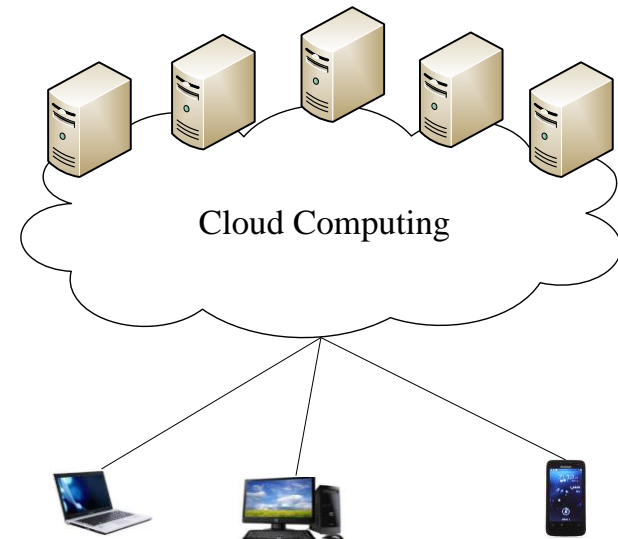


Computation in client:

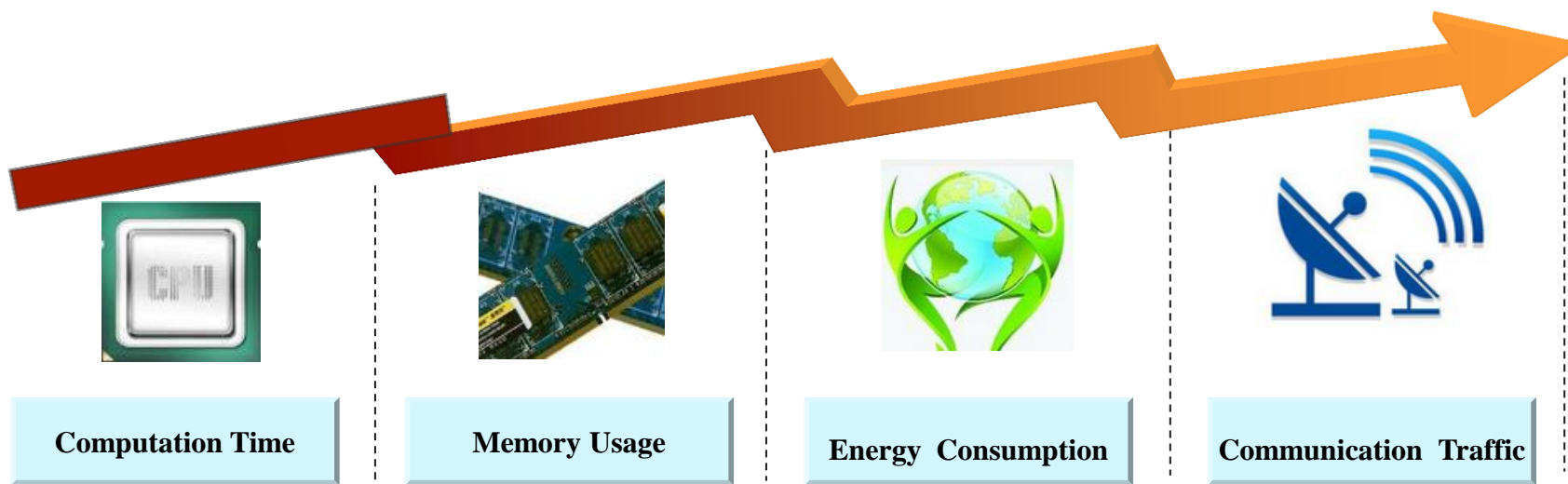
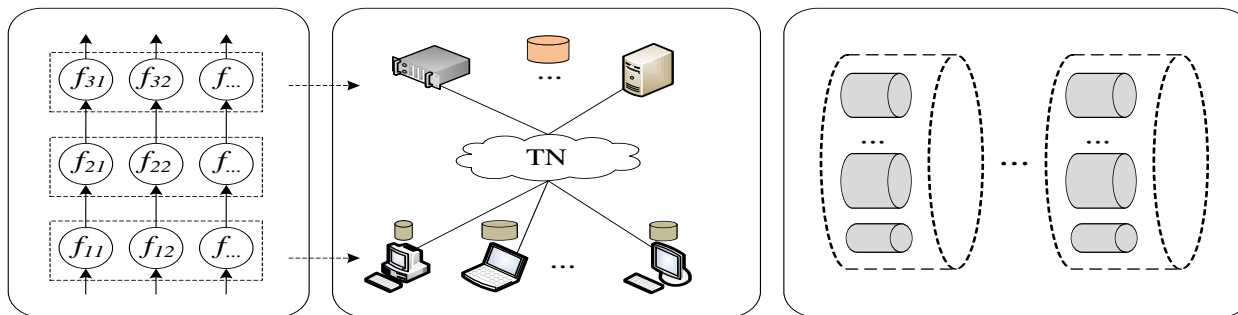
- SVD
- Incremental SVD

All computation are performed in sever

- SVD
- Incremental SVD
- Compute Core Tensor



Distributed Computing with Multi-Objective Optimization



$$OPT : \min Z = \beta_1 Tim + \beta_2 Mem + \beta_3 Egy + \beta_4 Tra$$

A Tensor-Based Approach

3.1

- Tensor and Tensor Decomposition

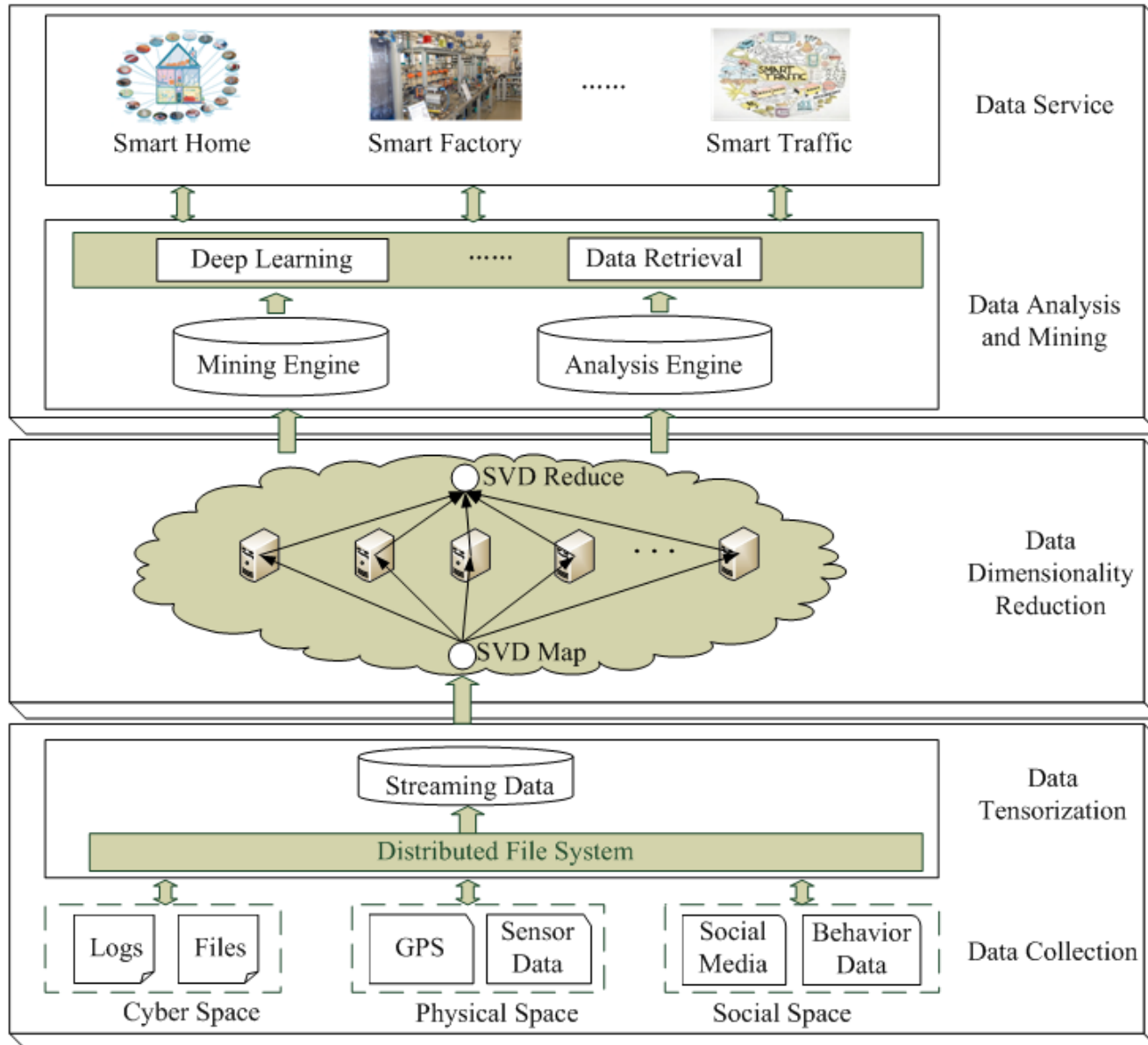
3.2

- ‘4Vs Problem’ with Tensor

3.3

- A Framework for Big Data Analysis and Mining

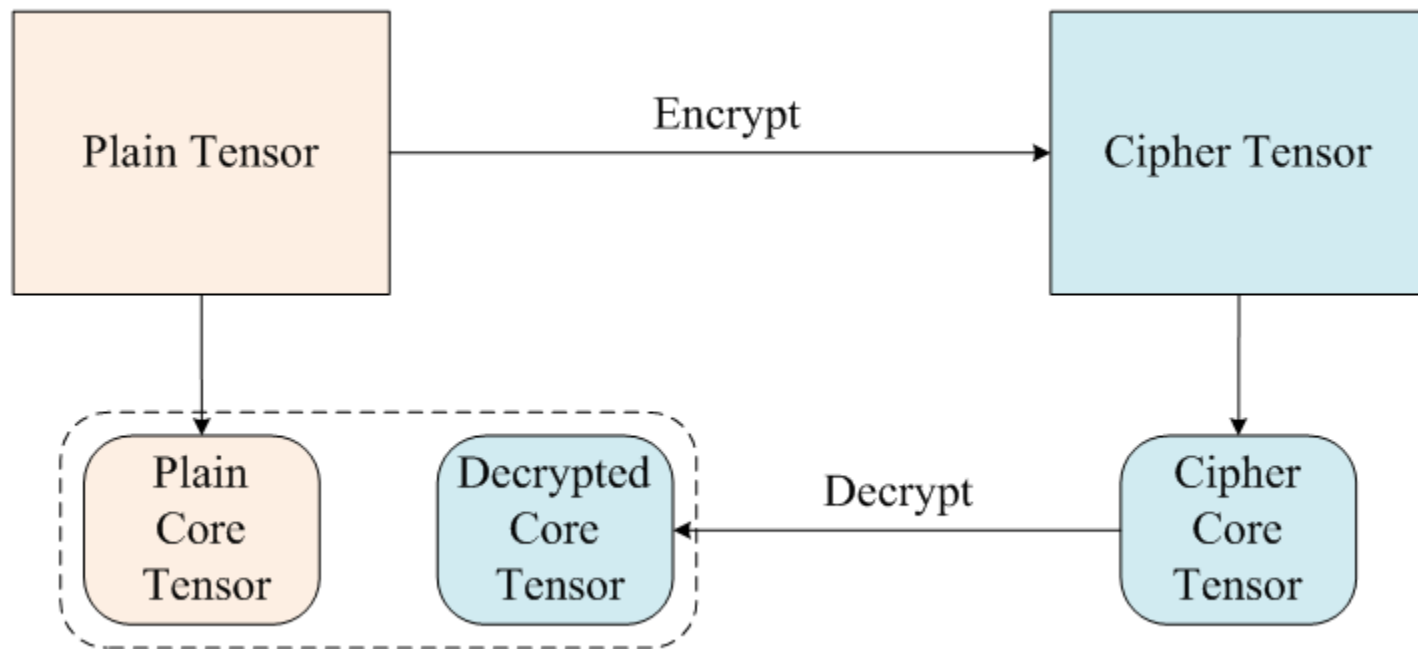
Big Data Framework



The Framework

1. Secure Dimensionality Reduction
2. A Deep Computation Model
3. Big Data Ranking and Retrieval
4. A Promising Technique: Fuzzy Tensor

1. Secure Dimensionality Reduction



1. Secure Dimensionality Reduction

Paillier Encryption. Paillier encryption is a partially homomorphic encryption scheme which is more efficient than the fully homomorphic schemes. The encryption and decryption procedure are defined as follows:

$$c = g^m \cdot r^n \text{ mod } n^2,$$

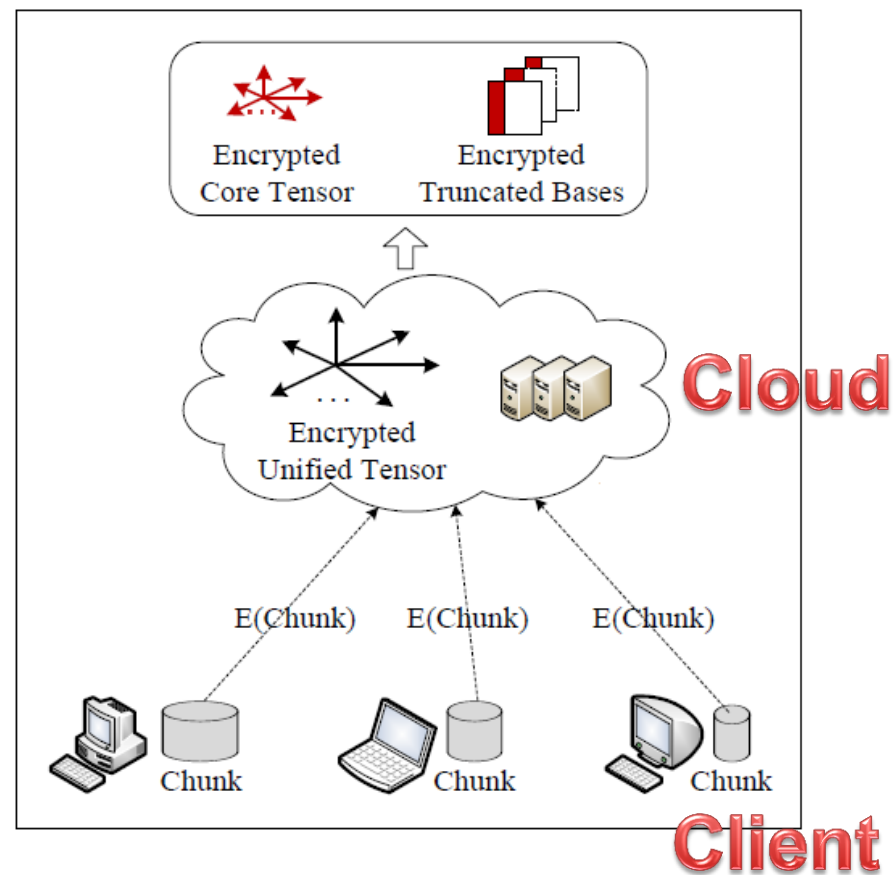
$$m = \frac{L(c^\lambda \text{ mod } n^2)}{L(g^\lambda \text{ mod } n^2)} \text{ mod } n.$$

The public key cryptosystem is based on the composite degree residuosity classes. It preserves homomorphic addition and multiplication that can be described as

$$E(x) + E(y) = E(x + y),$$

$$E(xy) = (E(x))^y \text{ mod } n^2.$$

No.	Operation	Homomorphic
1	+	yes
2	-	yes
3	×	yes
4	÷	no
5	\sqrt{x}	no
6	<i>mod</i>	no



1. Secure Dimensionality Reduction

Algorithm 1 Secure Lanczos Iteration on Cloud.

Input:

A symmetric matrix $M \in R^{n \times n}$.

Output:

The Eigen Values and Eigen Vectors.

- 1: Select two vectors $w_1 \in R^n, v_1 \in R^n$ where $w_1^T v_1 = 1$.
 - 2: Compute $v = Mv_1, w = M^T w_1$;
 - 3: **for** j from 1 to k **do**
 - 4: Compute $\alpha_j = w_j^T v, v = v - \alpha_j v_j, w = w - \alpha_j w_j$.
 - 5: **if** $\|v\|_2 = 0$ or $\|w\|_2 = 0$ **then**
 - 6: Exit.
 - 7: **else**
 - 8: Compute $w_j = v^T w$.
 - 9: **end if**
 - 10: **if** $w_j = 0$ **then**
 - 11: Exit.
 - 12: **else**
 - 13: Send w_j, v, w to Client.
 - 14: Receive $\beta_j, \gamma_j, v_{j+1}, w_{j+1}$ from Client.
 - 15: **end if**
 - 16: $v = Av_{j+1} - \gamma_j v_j; w = A^T w_{j+1} - \beta_j w_j$.
 - 17: **end for**
 - 18: Obtain the Tridiagonal Matrix
 - 19: Send the Tridiagonal Matrix to Client.
-

Algorithm 2 Secure Lanczos Iteration on Client.

Input:

Middle results from Cloud.

Output:

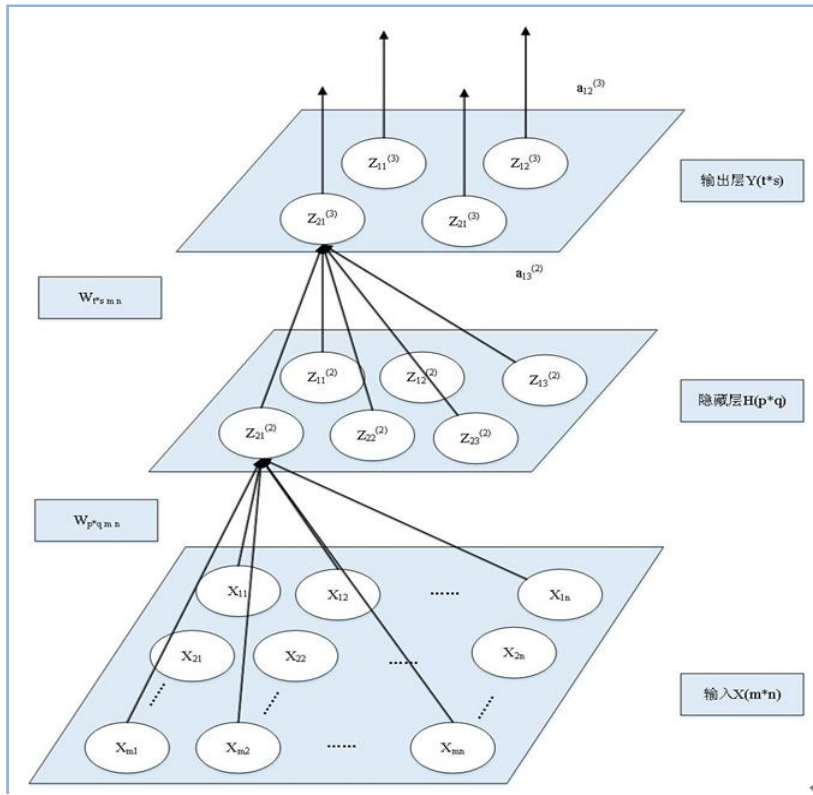
Processed Middle Results.

- 1: Receive w_j, v, w from Cloud.
 - 2: $\beta_j = \sqrt{|w_j|}; \gamma_j = w_j / \beta_j$.
 - 3: $v_{j+1} = v / \beta_j; w_{j+1} = w / \gamma_j$.
 - 4: Send $\beta_j, \gamma_j, v_{j+1}, w_{j+1}$ to Cloud.
 - 5: Receive the Tridiagonal Matrix from Cloud.
 - 6: Compute the Core Tensor and Truncated Bases.
-

2. Big Data + Tensor + Deep Learning = Deep Computation

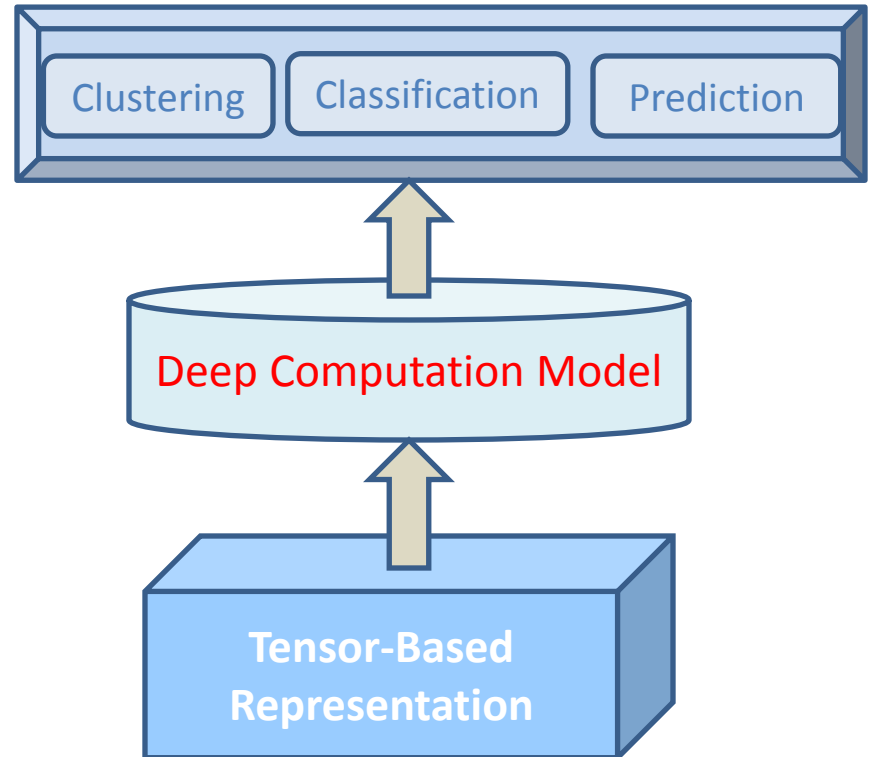
Deep Computation Model:

- Input/Output: Tensor-Based Data
- Hidden: Tensor-Based Features
- Parameter: Tensor-Based Parameters



Deep Computation Model:

- A General Deep Learning Model for Big Data
- Unsupervised Feature Learning
- Bridge Between Representation and Mining



2. Big Data + Tensor+ Deep Learning = Deep Computation

Deep Computation Model:

- Input/Output: Tensor-Based Data
- Hidden: Tensor-Based Features
- Parameter: Tensor-Based Parameters

(1) input layer → hidden layer: \circ

$$H = f_{\theta}(W^{(1)} \circ X + b^{(1)})$$

$$\theta = \{W^{(1)}, b^{(1)}\}, W^{(1)} \in R^{\alpha \times I_1 \times I_2 \times \dots \times I_n}, b^{(1)} \in R^{J_1 \times J_2 \times \dots \times J_n}$$

$$\alpha = J_1 \times J_2 \times \dots \times J_n$$

(2) hidden layer → output layer: \circ

$$h_{W,b}(X) = f_{\theta'}(W^{(2)} \circ H + b^{(2)})$$

$$\theta' = \{W^{(2)}, b^{(2)}\}, W^{(2)} \in R^{\beta \times J_1 \times J_2 \times \dots \times J_n}, b^{(2)} \in R^{K_1 \times K_2 \times \dots \times K_n}$$

$$\beta = K_1 \times K_2 \times \dots \times K_n$$

Deep Computation Model

- Tensor-Based Computing
- Tensor Distance → Data Distribution
- Cost Function → Tensor Distance

$$J(W, b) = \left[\frac{1}{m} \sum_{i=1}^m J(W, b; X^{(i)}, Y^{(i)}) \right] + \frac{\lambda}{2} \left(\sum_{j=1}^{\alpha} \sum_{i_1=1}^{I_1} \sum_{i_2=1}^{I_2} \dots \sum_{i_n=1}^{I_n} (W_{i_1 i_2 \dots i_n}^{(1)})^2 \right)$$

$$+ \sum_{k=1}^{\gamma} \sum_{j_1=1}^{J_1} \sum_{j_2=1}^{J_2} \dots \sum_{j_n=1}^{J_n} (W_{j_1 j_2 \dots j_n}^{(2)})^2 + \beta \sum_{j_1=1}^{J_1} \sum_{j_2=1}^{J_2} \dots \sum_{j_n=1}^{J_n} (\rho || \hat{\rho}_{j_1 j_2 \dots j_n})$$

$$J(W, b; X^{(i)}, Y^{(i)}) = \frac{1}{2} d_{TD}^2(X^{(i)}, Y^{(i)})$$

$$\alpha = J_1 \times J_2 \times \dots \times J_n; \gamma = K_1 \times K_2 \times \dots \times K_n$$

$$X \in R^{I_1 \times I_2 \times \dots \times I_n}; x_l = X_{i_1 i_2 \dots i_n} \quad (1 \leq i_j \leq I_j, 1 \leq j \leq n)$$

$$l = i_1 + \sum_{j=2}^n (i_j - 1) \prod_{0=1}^{j-1} I_0$$

$$d_{TD} = \sqrt{\sum_{l,m=1}^{I_1 \times I_2 \times \dots \times I_n} g_{lm} (x_l - y_l) (x_m - y_m)} = \sqrt{(x - y)^T G (x - y)}$$

$$g_{lm} = \frac{1}{2\pi\sigma^2} \exp\left\{-\frac{||p_l - p_m||_2^2}{2\sigma^2}\right\}$$

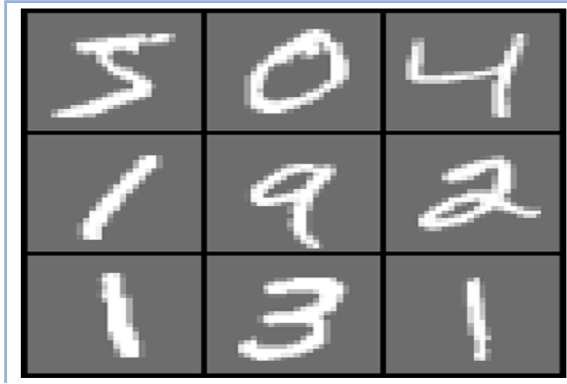
$$||p_l - p_m||_2 = \sqrt{(i_1 - i_1')^2 + (i_2 - i_2')^2 + \dots + (i_n - i_n')^2}$$



2. Big Data+Tensor+Deep Learning=Deep Computation Model

Deep Computation Model:

- Input/Output: Tensor-Based Data
- Hidden: Tensor-Based Features

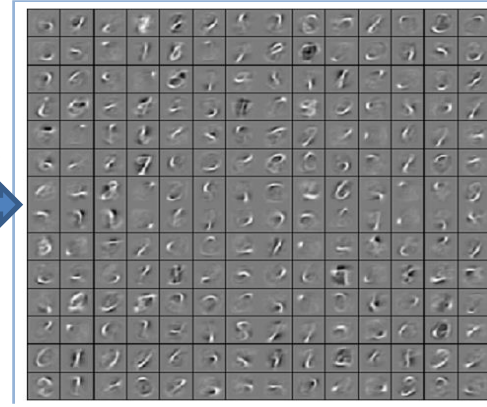


Edge Feature

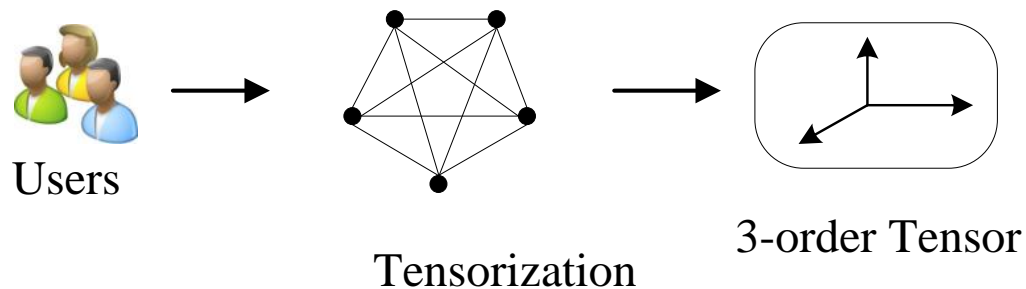
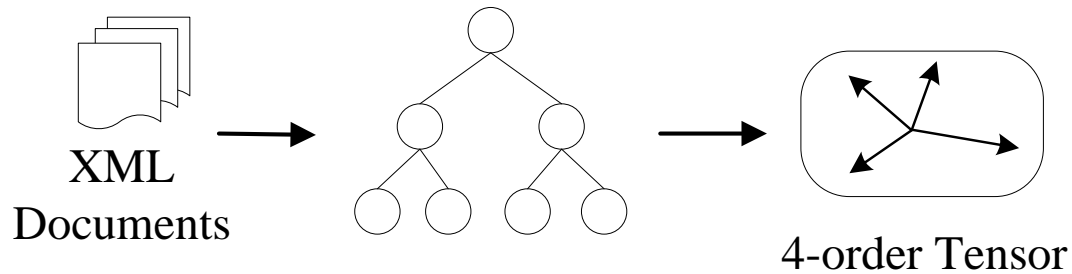
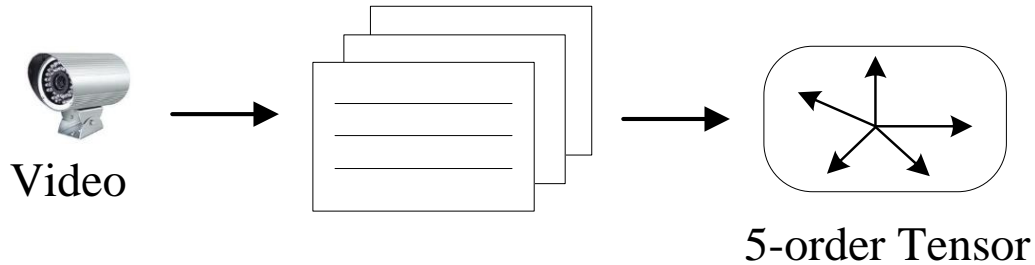
Color Feature

Deep Computation Model

- Unsupervised Feature Learning
- Bridge Between Representation and Mining

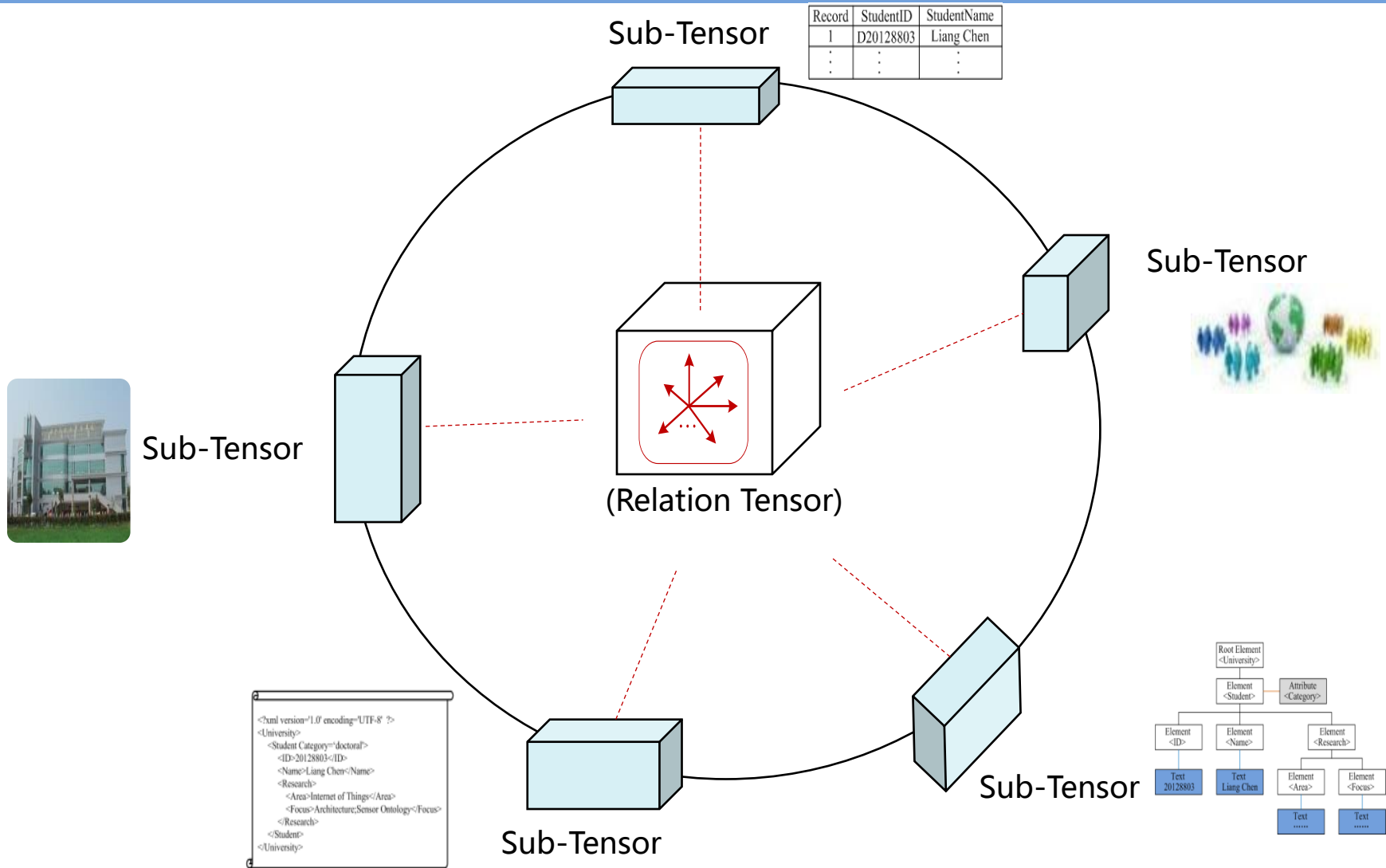


3. Big Data Ranking and Retrieval



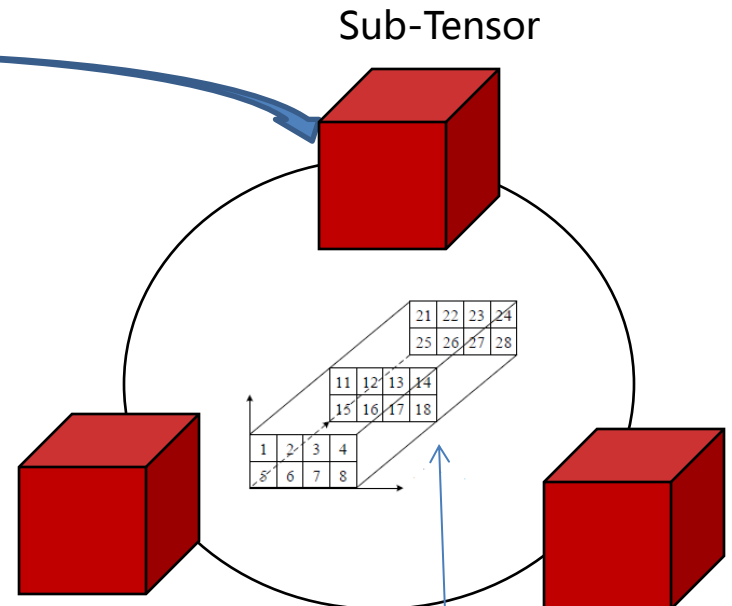
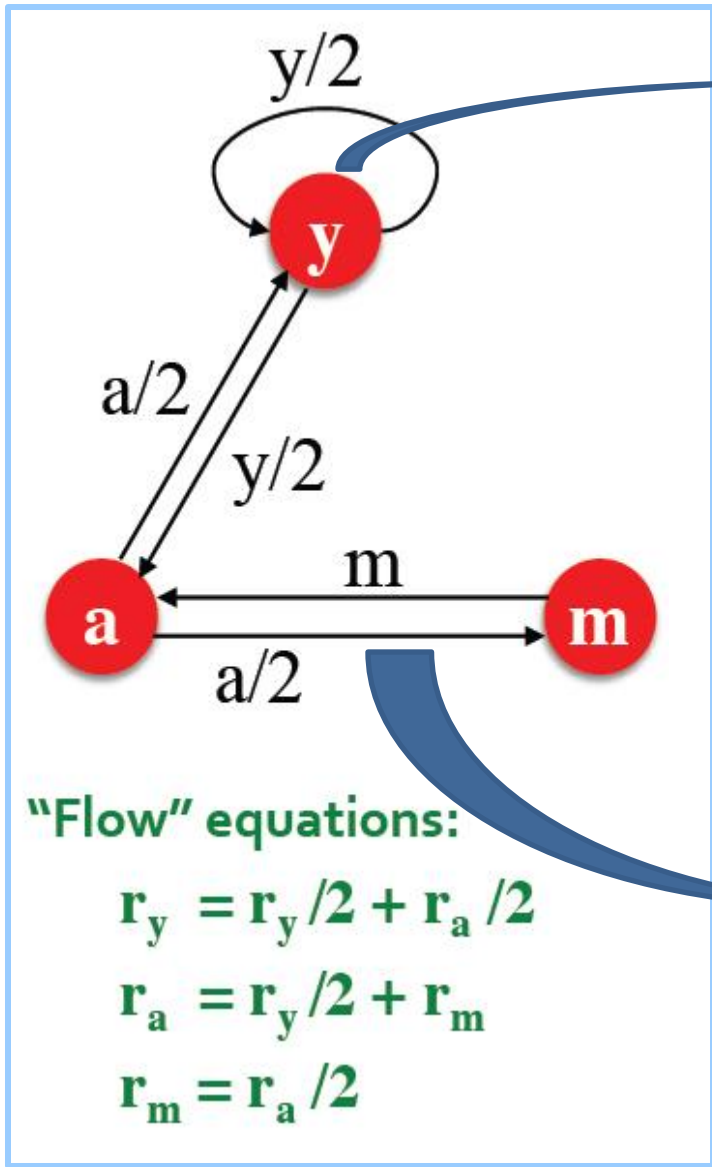
Data Space: Represent heterogeneous data as sub tensors.

3. Big Data Ranking and Retrieval



Metric Space: Map all the sub tensors to a Hamming Space, and obtain the similarity between all sub tensors. The similarities are stored in the relation tensor.

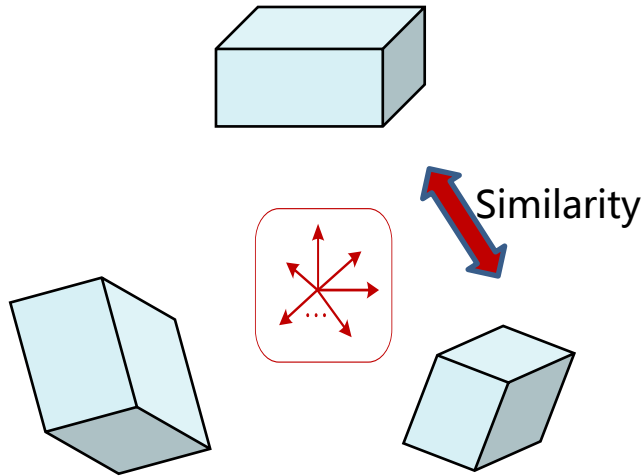
3. Big Data Ranking and Retrieval



$$r = T \times r$$

Vector r denotes the rank of the data object

3. Big Data Ranking and Retrieval



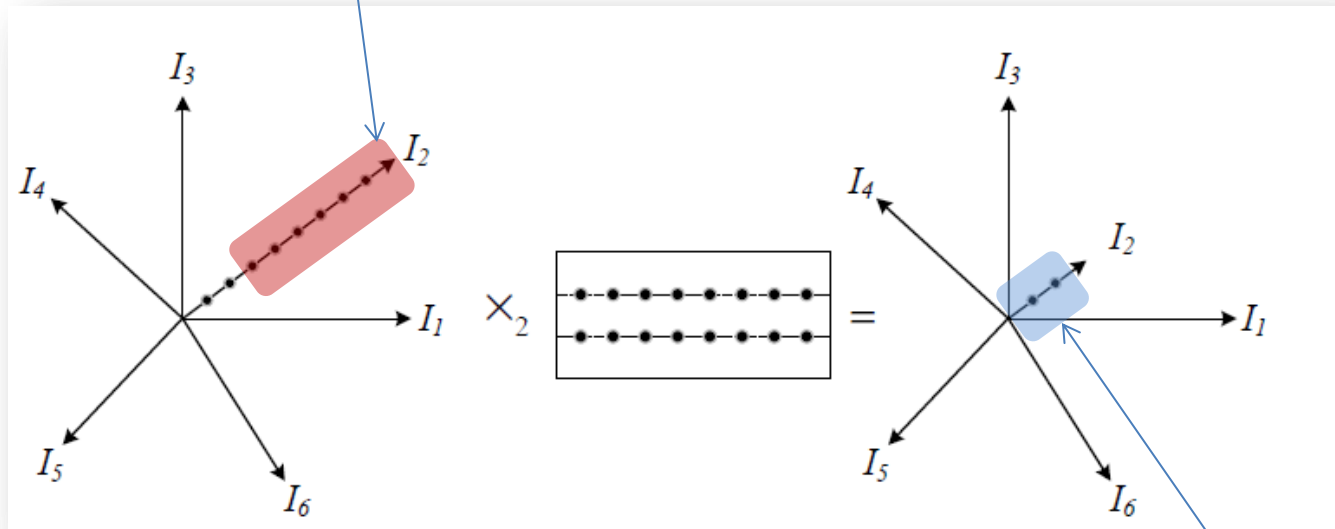
In the metric space, the similarity is computed with tensor distance.

Tensor Distance

$$d_{TD} = \sqrt{\sum_{l,m}^{I_1 \times I_2 \times \dots \times I_N} g_{lm} (x_l - y_l)(x_m - y_m)}$$
$$= \sqrt{(x - y)^T G (x - y)}$$

$$g_{lm} = \frac{1}{2\pi\sigma_1^2} \exp\left\{ \frac{-\|P_l - P_m\|_2^2}{2\sigma_1^2} \right\}$$

Redundancy, Uncertainty, Inconsistency, Incompleteness



Extract the distinguish dimensions that can best capture the characteristics of big data

4. Fuzzy Tensor

Data Structure: $4V$

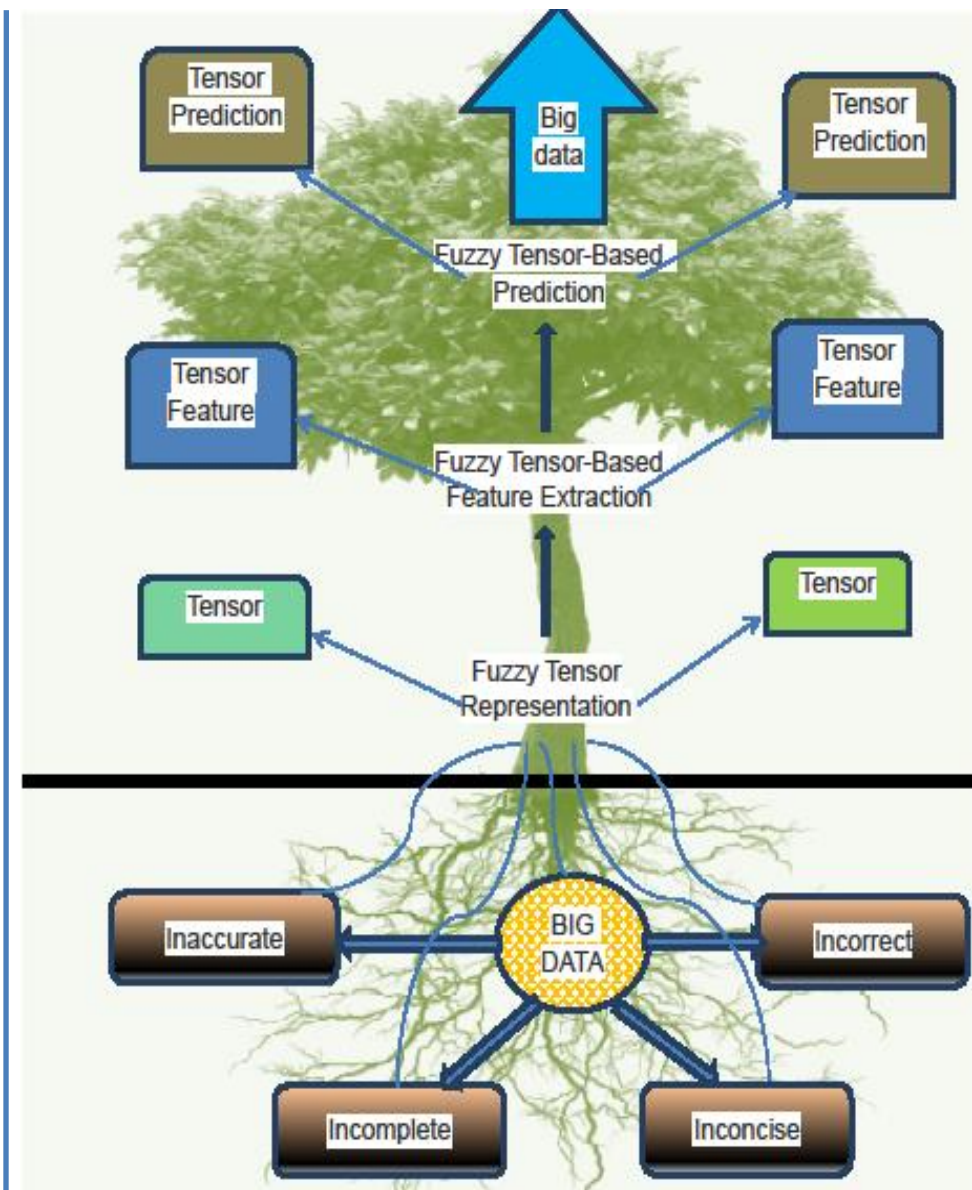


Data Feature: $4I$

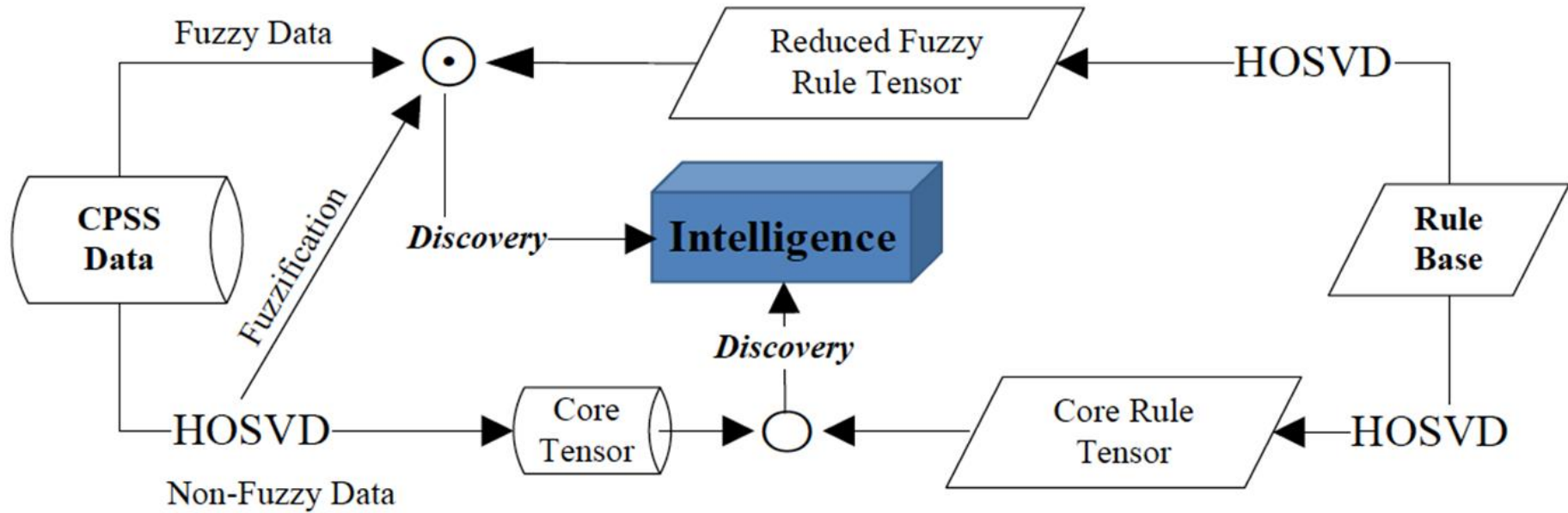
Tensor Generalization:

Tensor \rightarrow Fuzzy Tensor

What/How



4. Fuzzy Tensor





1. Smart Word and Hyper World

2. Big Data and Challenges

3. A Tensor-Based Approach

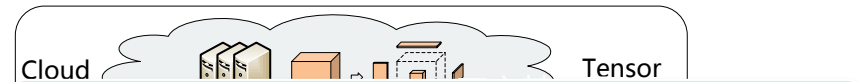
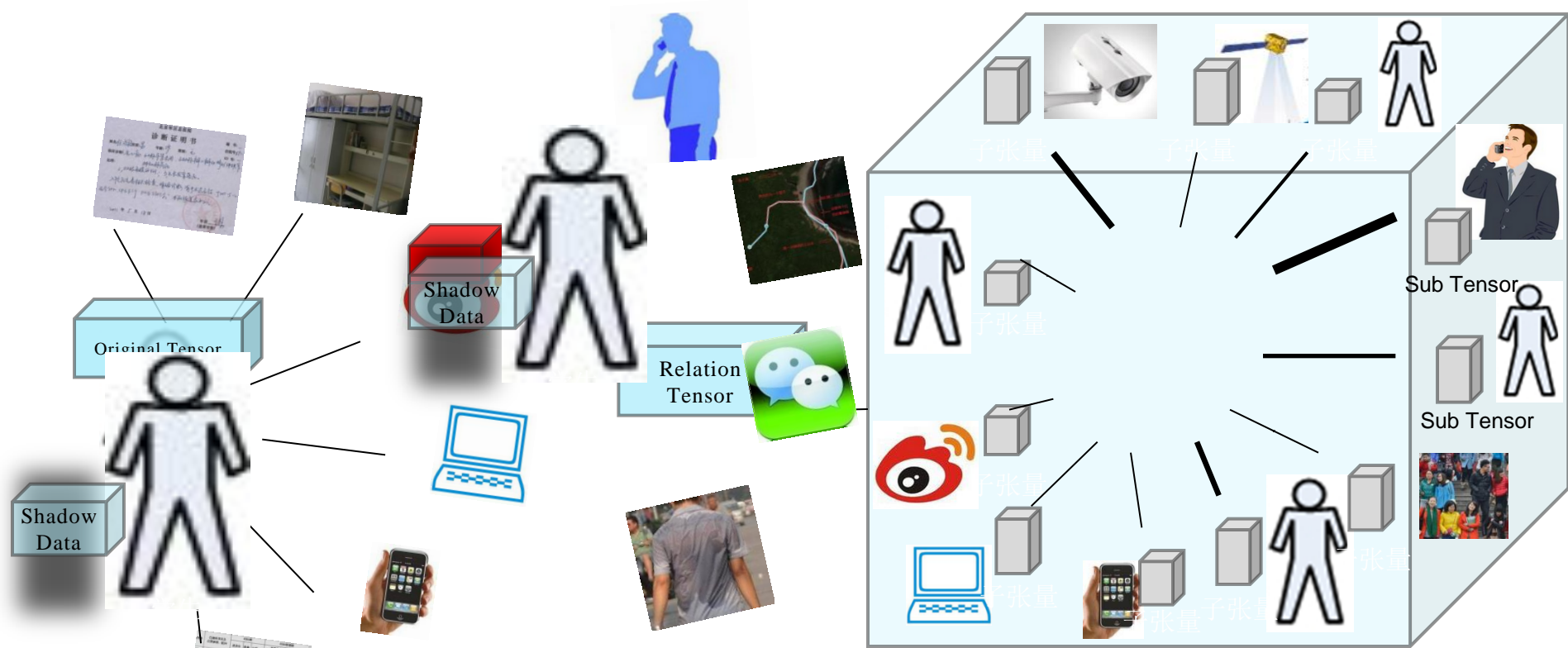
4. Illustration and Example

5. Conclusion

Illustration 1:

Smart City





• Deep Computation for Mining and Analysis
 $OPT : \min Z = \beta_1 F_1 + \beta_2 F_2 + \dots + \beta_n F_n$

$$f : (d_u \cup d_{semi} \cup d_s) \rightarrow \underbrace{T_u \cup T_{semi} \cup T_s}_T$$

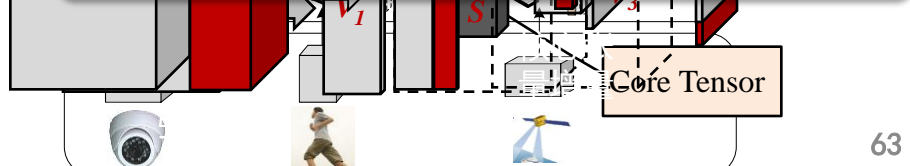
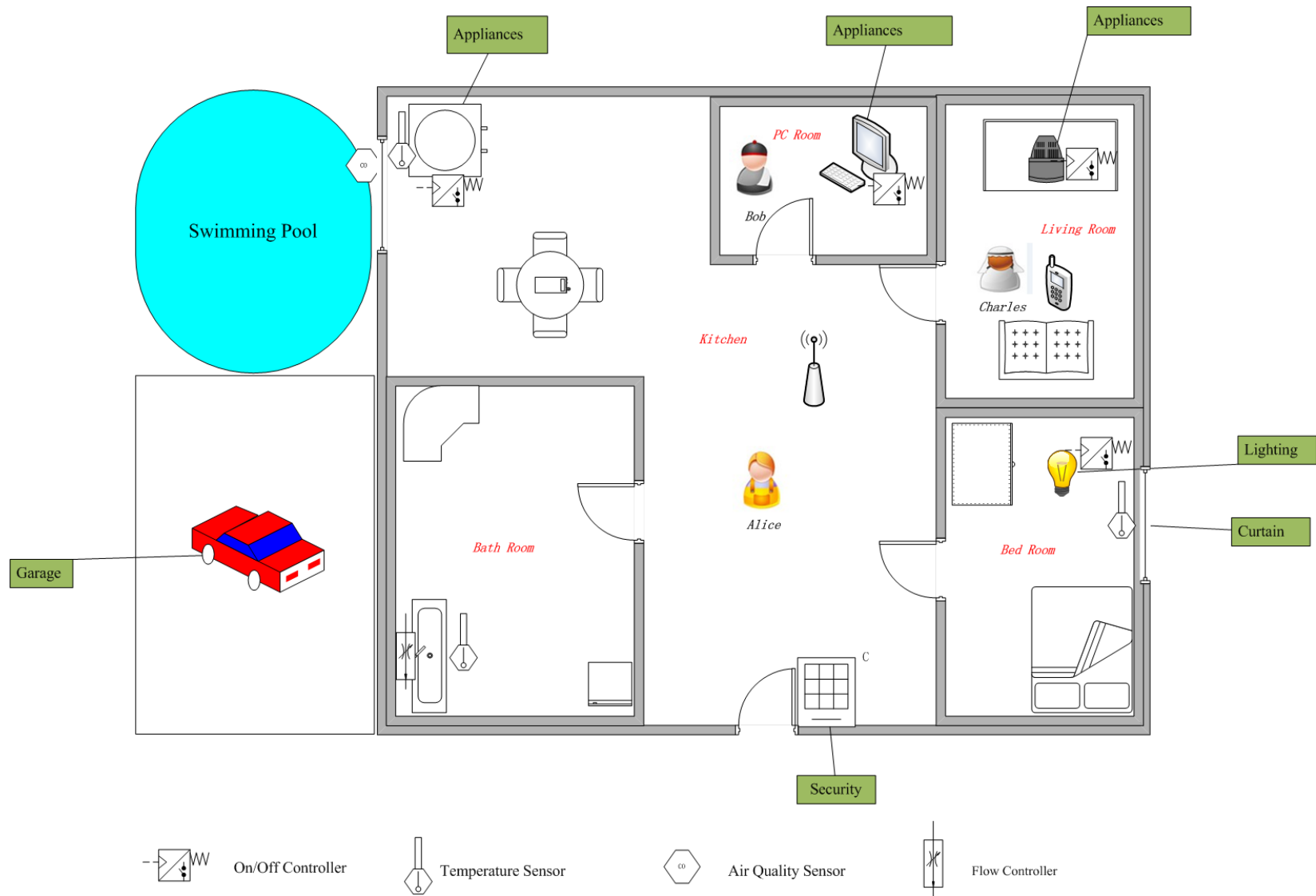


Illustration 2:

Smart Home



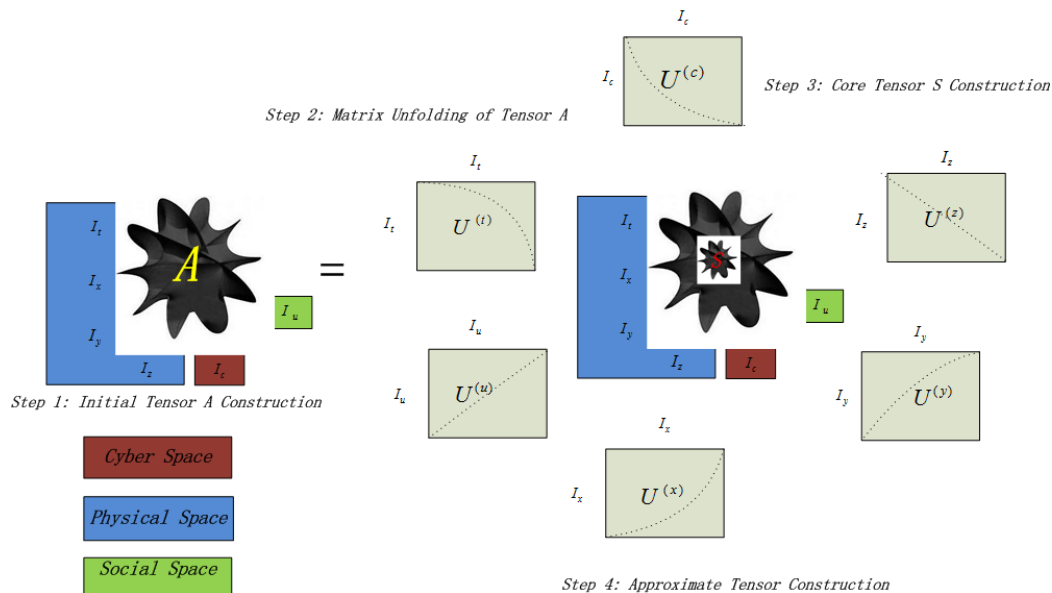
Heterogeneous Data from Intelligent Device



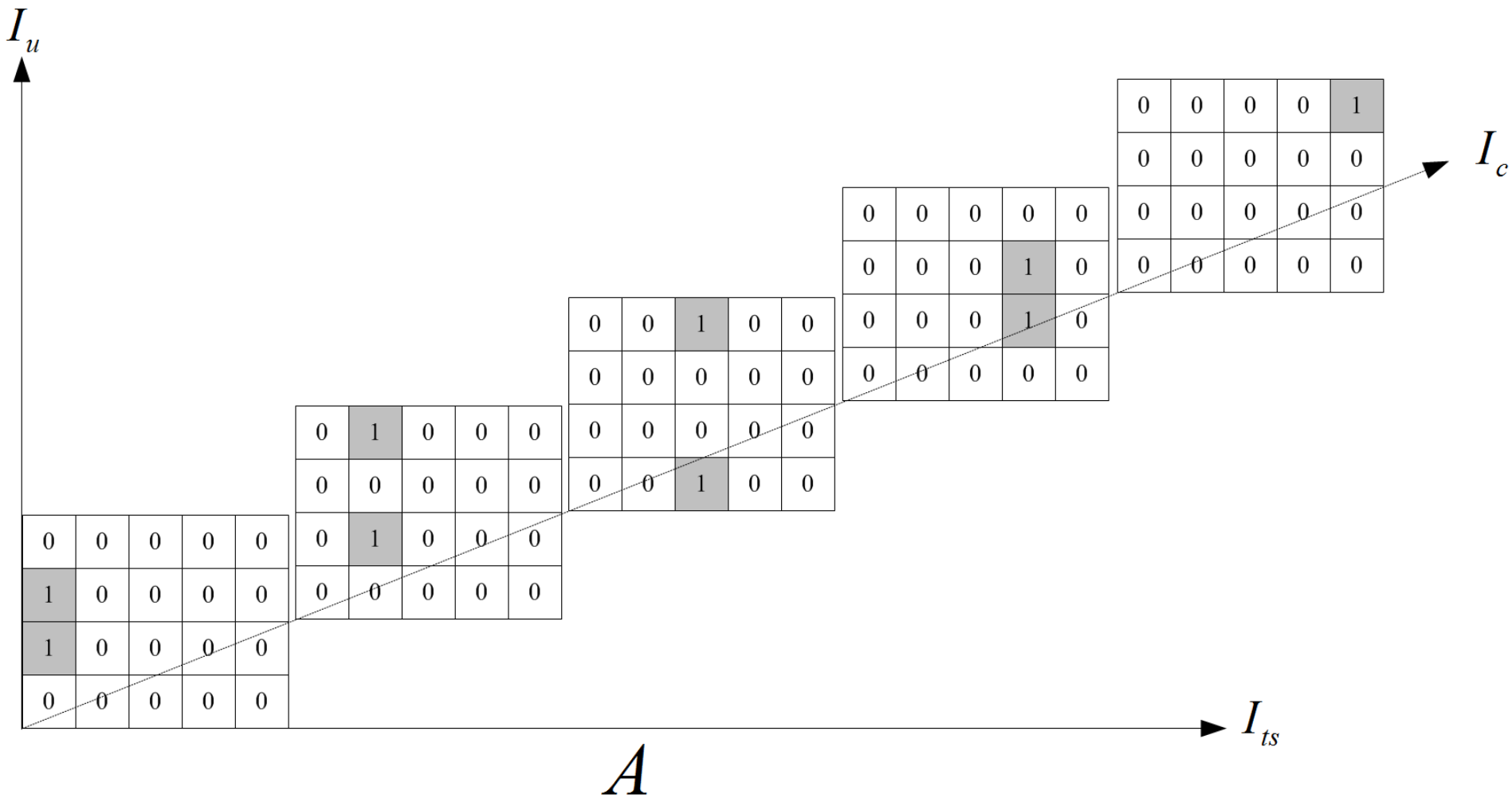
Four Step to Construct Six-Order Tensor

Smart Home

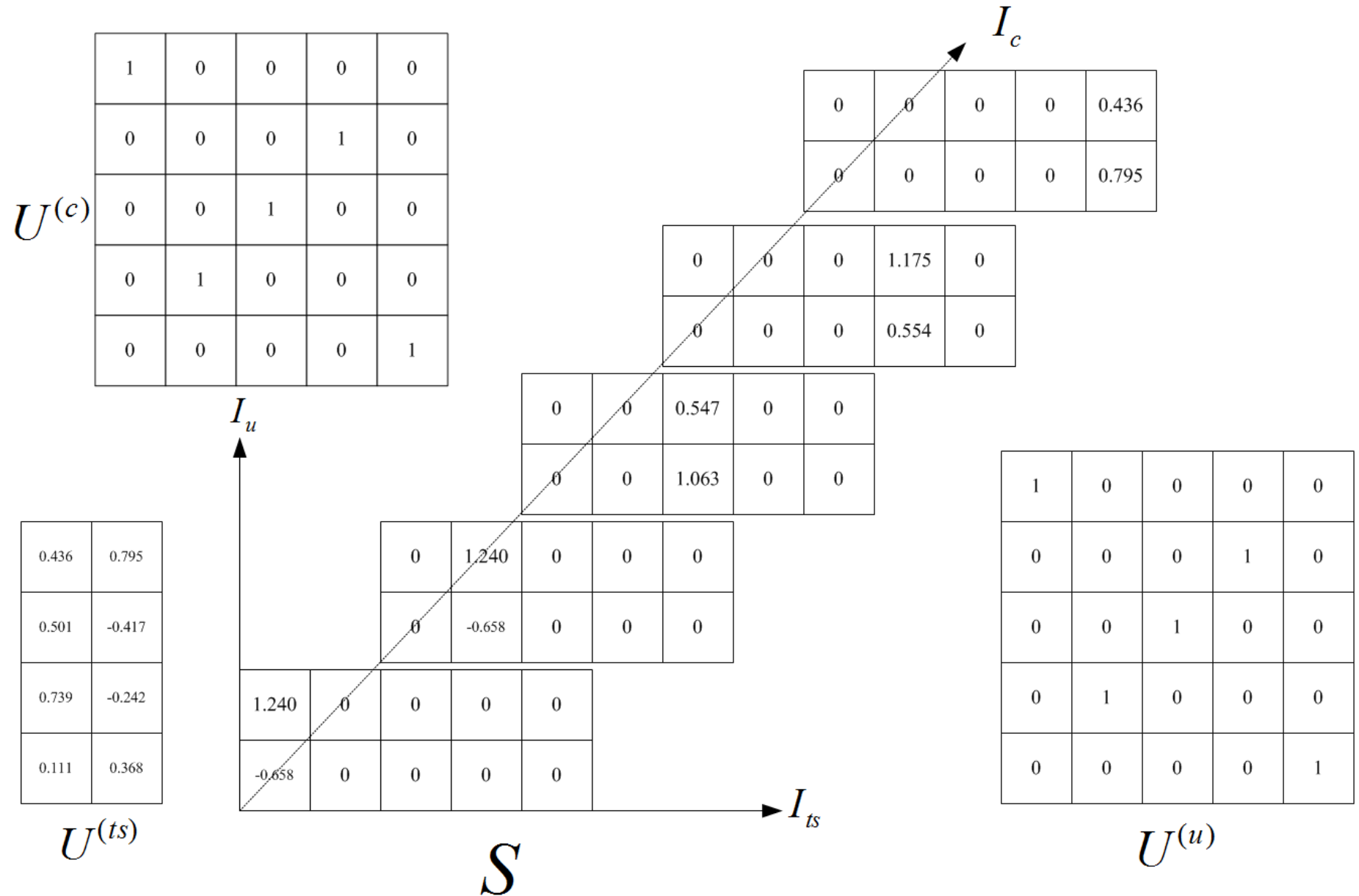
- *Social Space: Father, Mother, Children...*
- *Physical Space: Bedroom, Dining room...*
- *Cyber Space: Computer, Electronic devices...*



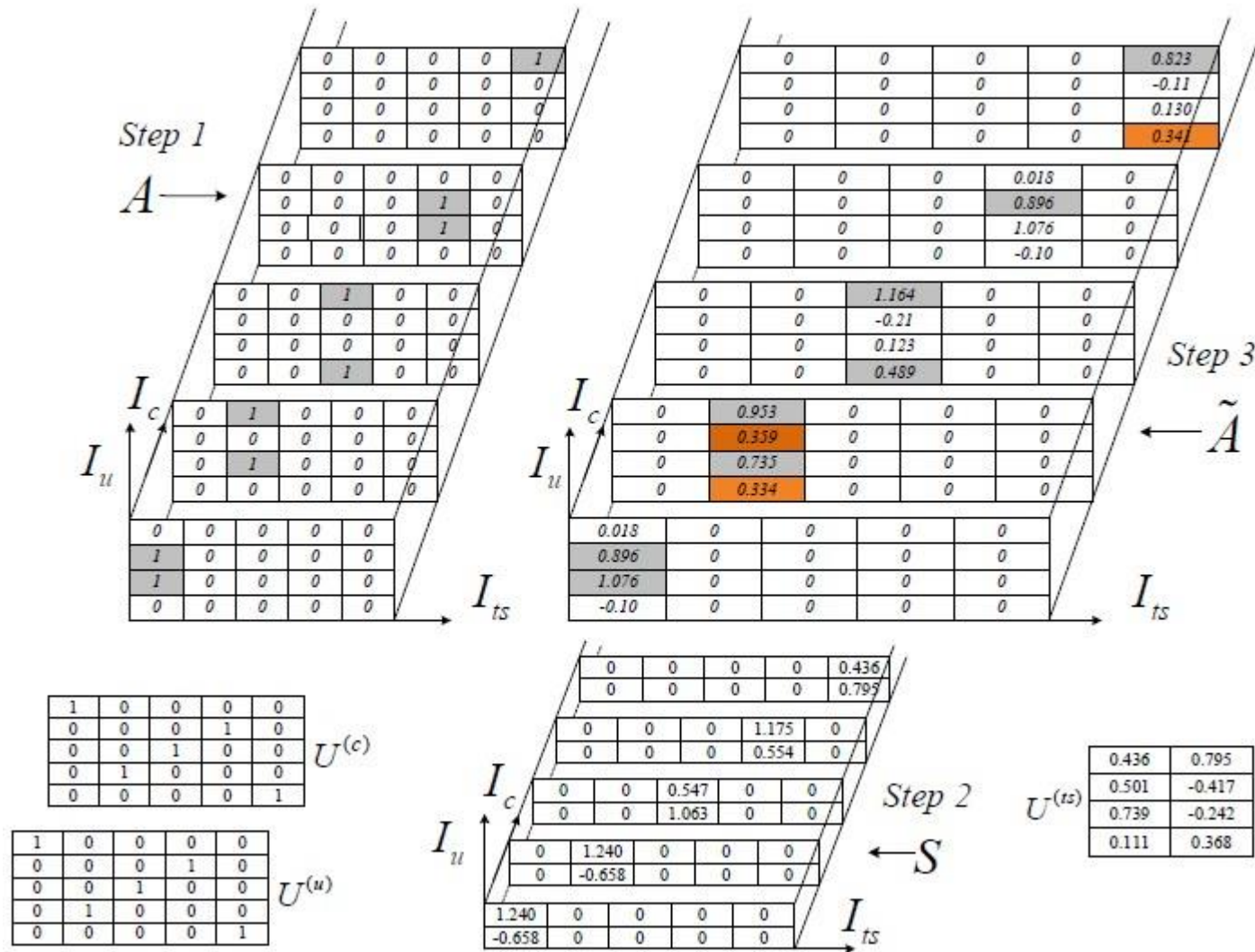
Initial Tensor



Tensor Decomposition



Approximate Tensor Construction



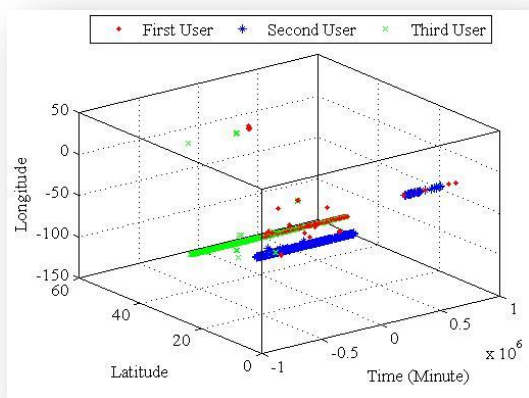
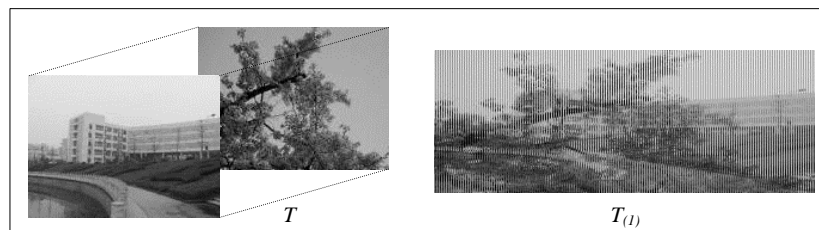
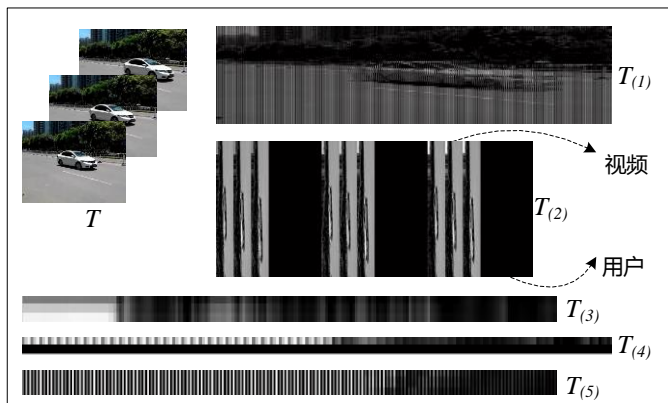
Likelihood Generated by Approximation Tensor

Record	User	Time & Space	Cyber Resource	Weight 1	Weight 2
1	Charles	6:00PM, Living Rm.	$TV_{on}=1$	1	0.896
2	Lucy	6:30PM, Swim.Pool	$Faucet_{on}=1$	1	0.823
3	Alice	7:10PM, Kitchen	$Pot_{on}=1$	1	1.076
4	Lucy	8:00PM, PC Rm.	$PC_{on}=1$	1	1.164
5	Alice	8:00PM, Living Rm.	$TV_{on}=1$	1	1.076
6	Charles	9:00PM, Kitchen	$Pot_{on}=1$	1	0.896
7	Lucy	9:30PM, Bed Rm.	$LE_{off}=1$	1	0.953
8	Alice	10:10PM, Bed Rm.	$LE_{off}=1$	1	0.735
9	Bob	11:30PM, PC Rm.	$PC_{on}=1$	1	0.489
10	Charles	10:10PM, Bed Rm.	$LE_{off}=1$	-	0.359
11	Bob	9:30PM, Bed Rm.	$LE_{off}=1$	-	0.334
12	Bob	6:30PM, Swim.Pool	$Faucet_{on}=1$	-	0.341

Published Research Work



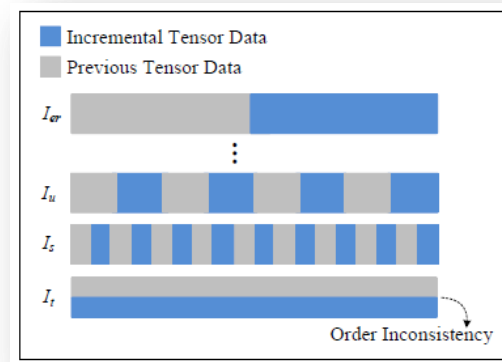
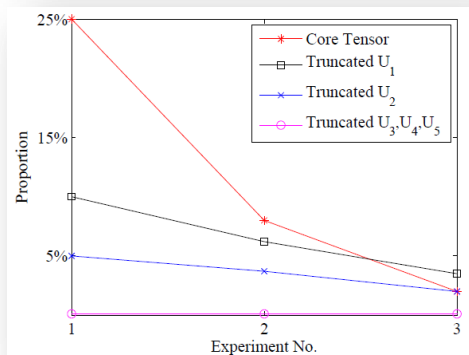
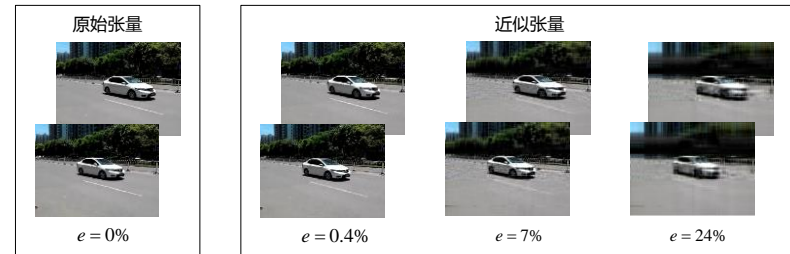
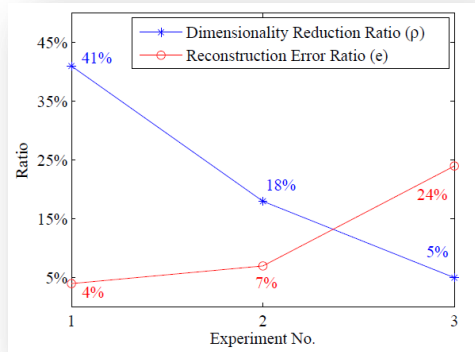
Unified Representation Model for Big Data



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    <ID>20128803</ID>
    <Name>Liang Chen</Name>
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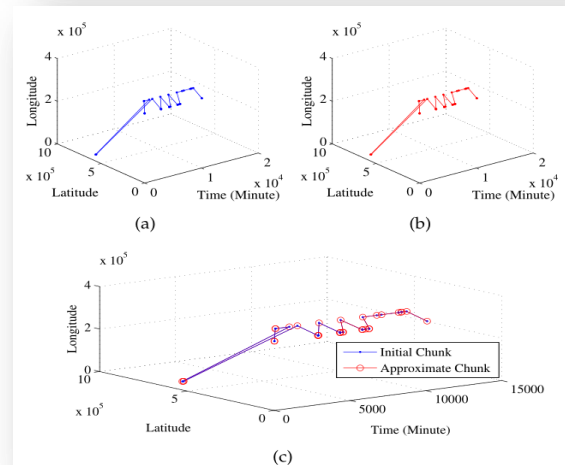
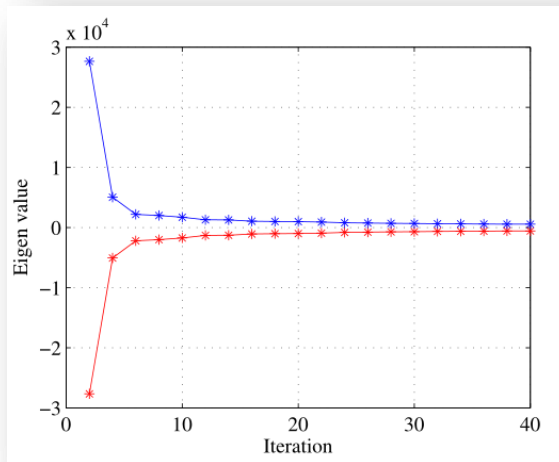
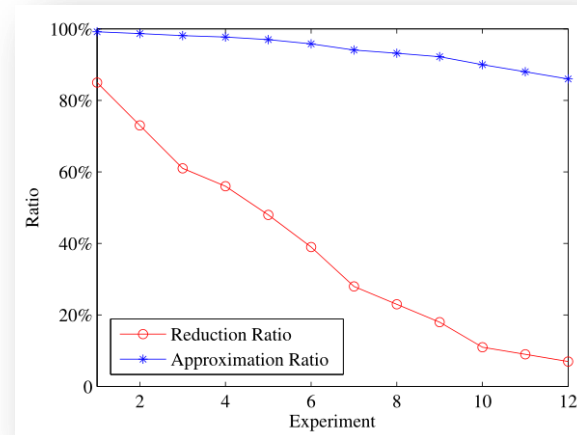
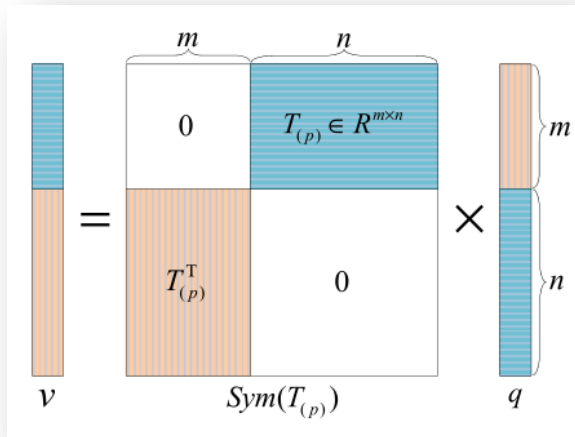
L. Kuang, F. Hao, L.T. Yang, M. Lin, C. Luo and G. Min, "A Tensor-Based Approach for Big Data Representation and Dimensionality Reduction", IEEE Transactions on Emerging Topics in Computing (TETC), 2014, DOI: 10.1109/TETC.2014.2330516.

Incremental HOSVD



L. Kuang, F. Hao, L.T. Yang, M. Lin, C. Luo and G. Min, "A Tensor-Based Approach for Big Data Representation and Dimensionality Reduction", IEEE Transactions on Emerging Topics in Computing (TETC), 2014, DOI: 10.1109/TETC.2014.2330516.

Distributed Dimensionality Reduction of Big Data



L. Kuang, Y. Zhang, L.T. Yang, J. Chen, F. Hao, and C. Luo, "A Holistic Approach to Distributed Dimensionality Reduction of Big Data", IEEE Transactions on Cloud Computing (TCC), 2014, Accepted.



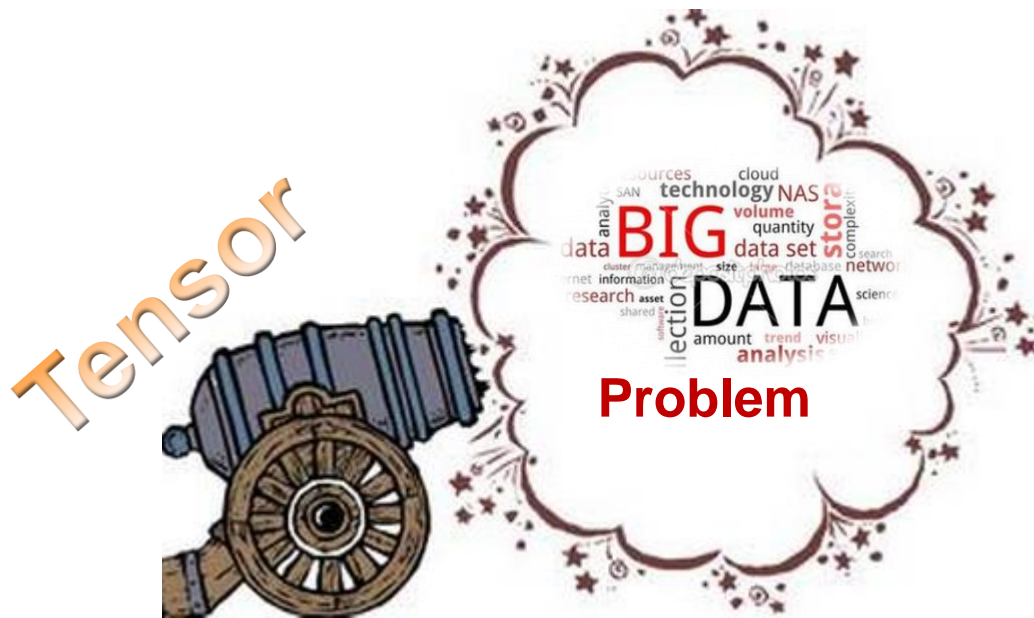
1. Smart Word and Hyper World

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5. Conclusion



A tensor-based framework for big data **Representations, Relations, Reductions, Retrieval, Reasoning and Recommendations!**